

Electronic structure, atomic forces and structural relaxations by WIEN2k

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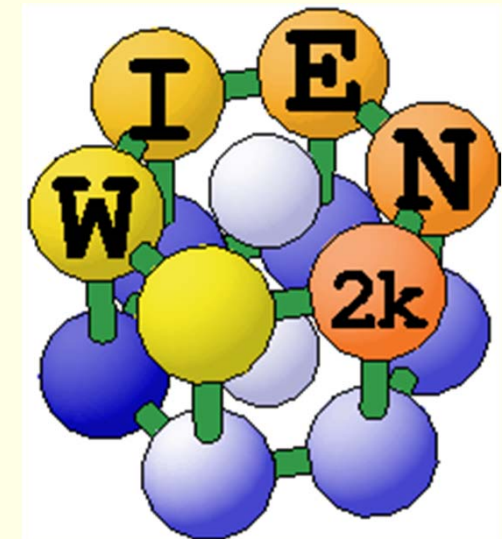
R.Laskowski, F.Tran, K.Schwarz (TU Vienna)

M.Perez-Mato (Bilbao)

K.Parlinski (Krakow)

D.Singh (Oakridge)

M.Fischer, T.Malcherek (Hamburg)





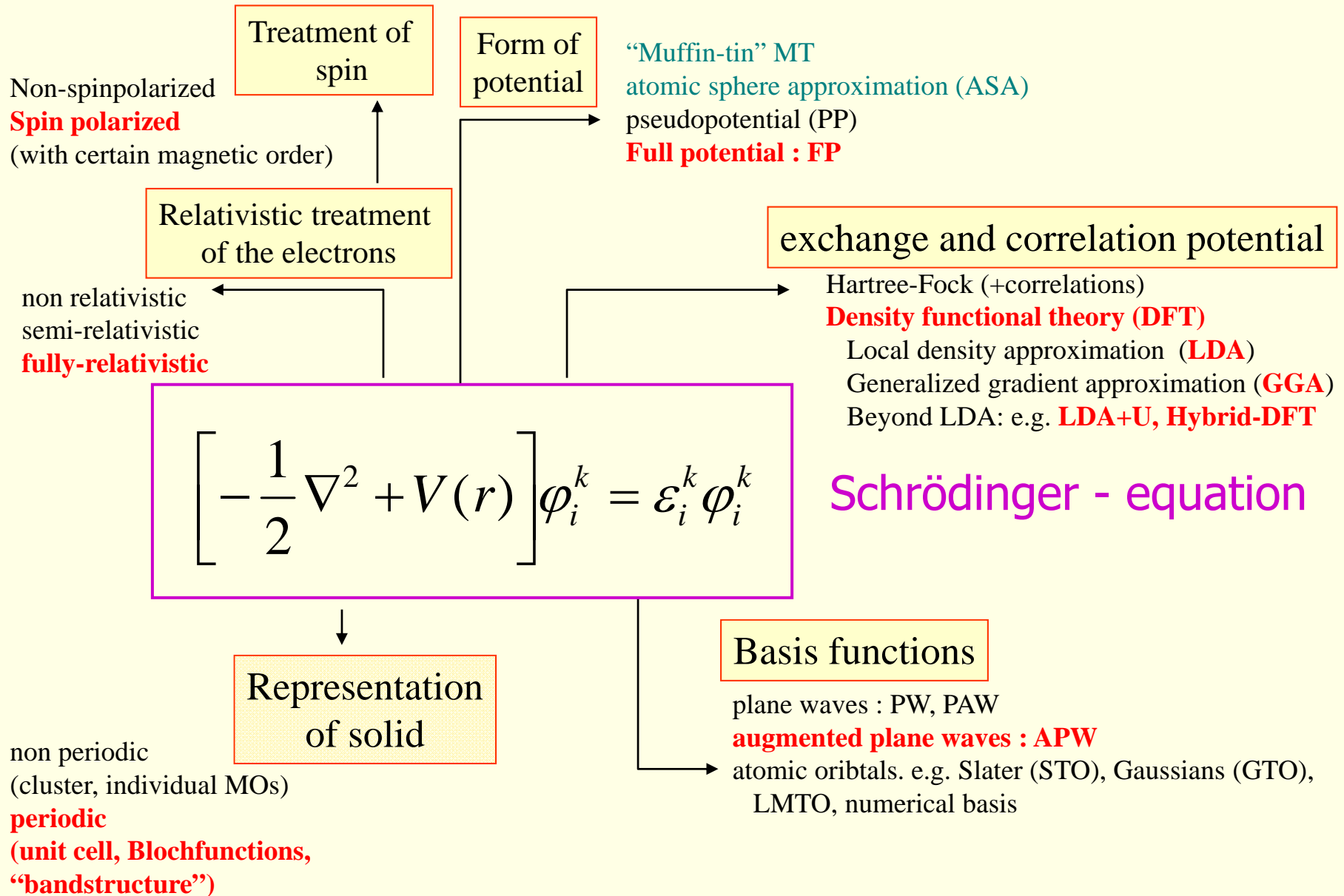
Outline:



- **General considerations when solving $H\Psi = E\Psi$**
 - *DFT*
 - *APW-based methods (history and state-of-the-art)*
 - *WIEN2k*
 - program structure + features
 - forces, structure relaxation
- **Applications**
 - *Phonons in matlockite PbFI*
 - *Phase transitions in Aurivillius phases*
 - *Structure of Pyrochlore $Y_2Nb_2O_7$*
 - *phase transitions in $Cd_2Nb_2O_7$*



Concepts when solving Schrödingers-equation





DFT Density Functional Theory



Hohenberg-Kohn theorem: (exact)

The total energy of an interacting inhomogeneous electron gas in the presence of an external potential $V_{\text{ext}}(\mathbf{r})$ is a **functional** of the density ρ

$$E = \int V_{\text{ext}}(\vec{r}) \rho(\vec{r}) d\vec{r} + F[\rho]$$

Kohn-Sham: (still exact!)

$$E = T_o[\rho] + \int V_{\text{ext}} \rho(\vec{r}) d\vec{r} + \frac{1}{2} \int \frac{\rho(\vec{r}) \rho(\vec{r}')}{|\vec{r}' - \vec{r}|} d\vec{r} d\vec{r}' + E_{xc}[\rho]$$

E_{kinetic}

non interacting

E_{ne}

E_{coulomb} E_{ee}

E_{xc} exchange-correlation

$$E_{xc}^{\text{LDA}} \propto \int \rho(r) \varepsilon_{xc}^{\text{hom.}}[\rho(r)] dr$$

$$E_{xc}^{\text{GGA}} \propto \int \rho(r) F[\rho(r), \nabla \rho(r)] dr$$

LDA

GGA

treats both, **exchange** and

correlation effects **approximately**



- Standard LDA (GGA) gives good description of most solids
- Problems:
 - *accuracy : functional "adapted" for specific materials or properties*
 - solids - molecules; metals - insulators - van der Waals bonds
 - geometry - binding energies
 - *"correlated" electrons: late 3d transition metal oxides/halides , 4f,5f e⁻*
 - metals instead of insulators (FeO, FeF₂, cuprates, ...)
 - nonmagnetic instead of anti-ferromagnetic (La₂CuO₄, YBa₂Cu₃O₆)
 - *band gaps in semiconductors/insulators*
 - gap typically underestimated by 50%



Is LDA repairable ?



ab initio methods

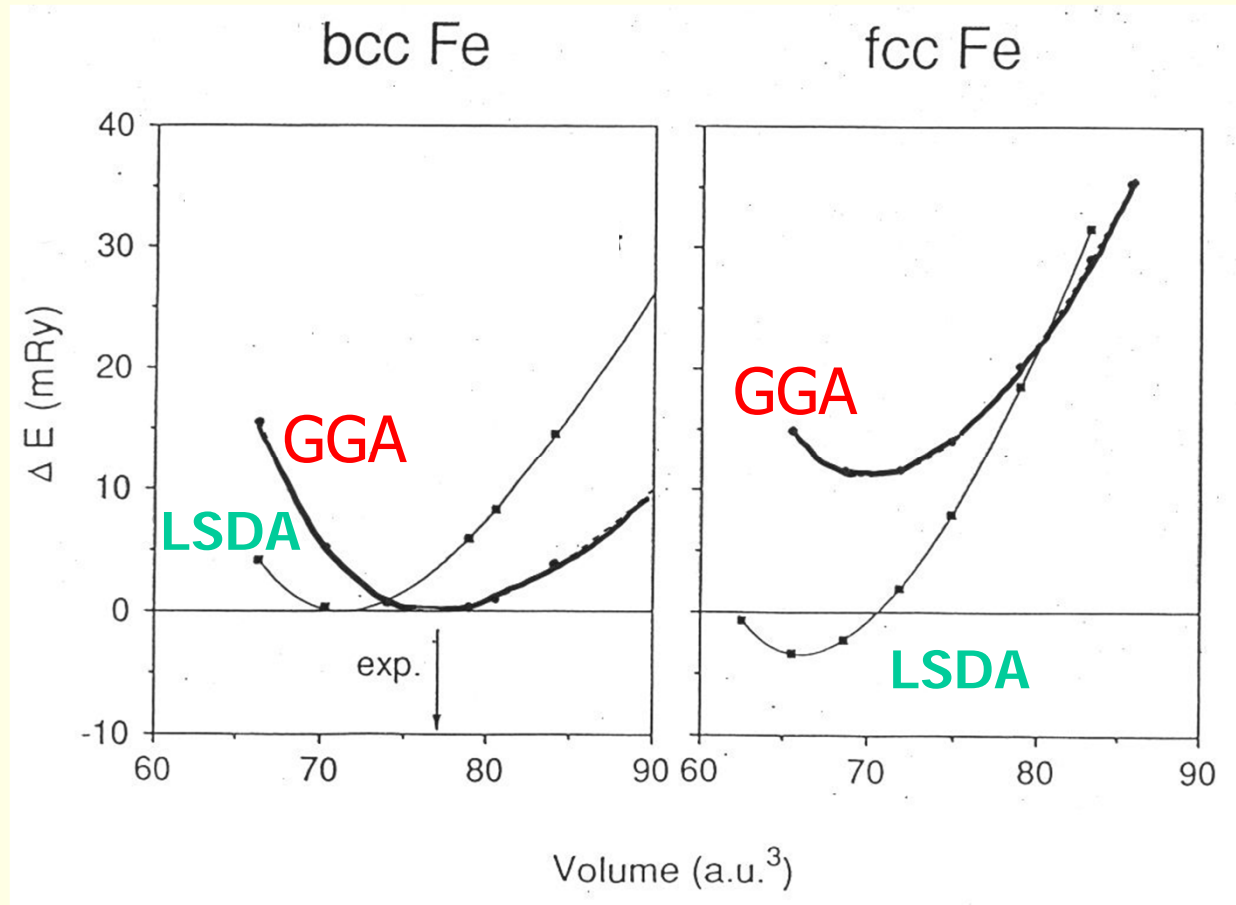
- **better GGAs and meta-GGAs ($\rho, \nabla\rho, \tau$):**
 - *usually improvement, but often too small.*
- **Exact exchange:** imbalance between exact X and approximate C
 - *hybrid-DFT (mixing of HF + GGA)*
 - *exact exchange + RPA correlation (extremely expensive)*
- **GW:** gaps in semiconductors, expensive!
- **Quantum Monte-Carlo:** very expensive

not fully ab initio

- **Self-interaction-correction:** vanishes for Bloch states
- **Orbital polarization:** Hund's 2nd rule by atomic Slater-parameter
- **LDA+U:** strong Coulomb repulsion via external Hubbard U parameter
- **DMFT:** extension of LDA+U for weakly correlated systems



DFT ground state of iron



- **LSDA** : Fe is a nonmagnetic metal with fcc structure (in contrast to experiment)
- **GGA**: Fe is a ferromagnetic metal with bcc structure (good lattice constant)

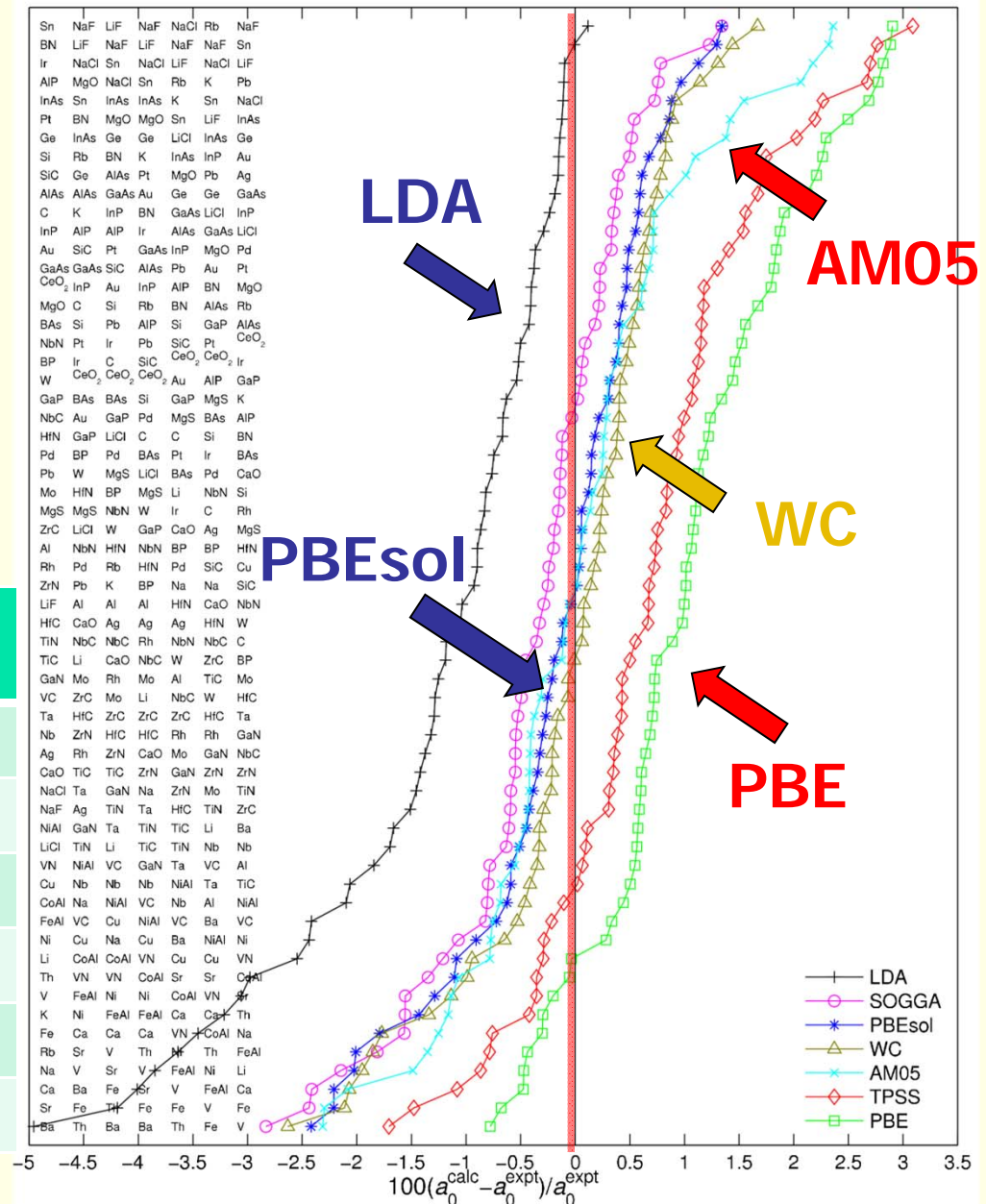


accuracy: "DFT limit"



- **Testing of DFT functionals:**
 - *error of theoretical lattice parameters for a large variety of solids (Li-Th)*

	me (Å)	mae (Å)	mre (%)	mare (%)
LDA	-0.058	0.058	-1.32	1.32
SO-GGA	-0.014	0.029	-0.37	0.68
PBEsol	-0.005	0.029	-0.17	0.67
WC	0.000	0.031	-0.03	0.68
AM05	0.005	0.035	0.01	0.77
PBE	0.051	0.055	1.05	1.18

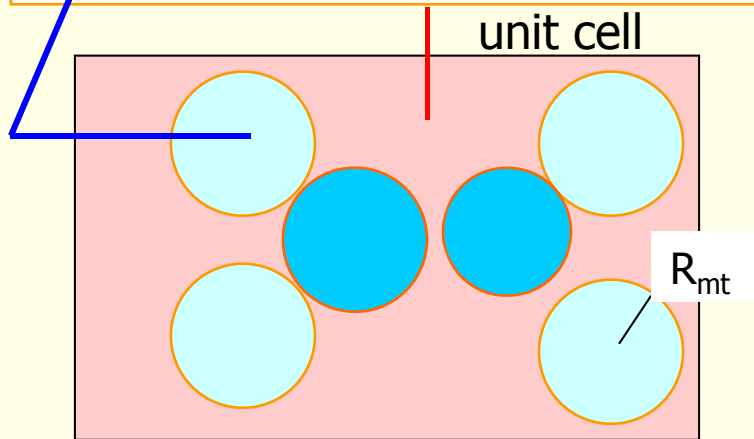




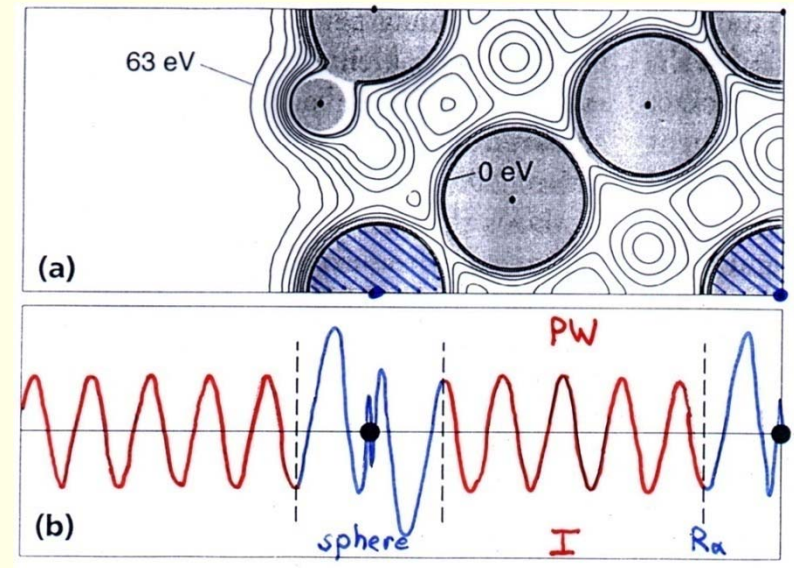
APW Augmented Plane Wave method



The unit cell is partitioned into:
atomic spheres
Interstitial region



Bloch wave function:
atomic partial waves
Plane Waves (PWs)



PW: $e^{i(\vec{k} + \vec{K}) \cdot \vec{r}}$

join

Atomic partial waves

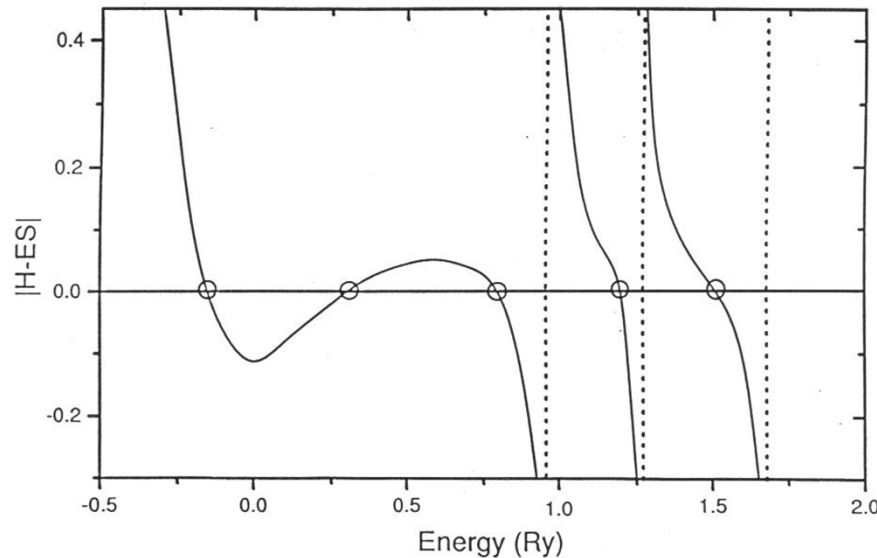
$$\sum_{lm} a_{lm}^K u_l(r', \epsilon) Y_{lm}(\hat{r}')$$

matching coefficient,

radial function, spherical harmonics



Slater's APW (1937)



Atomic partial waves

$$\sum_{\ell m} a_{\ell m}^K u_{\ell}(r', \varepsilon) Y_{\ell m}(\hat{r}')$$

Energy dependent

Radial basis functions lead to

H Hamiltonian
S Overlap matrix

Non-linear eigenvalue problem

Numerically search for the energy, for which $\det|H-ES|$ vanishes.

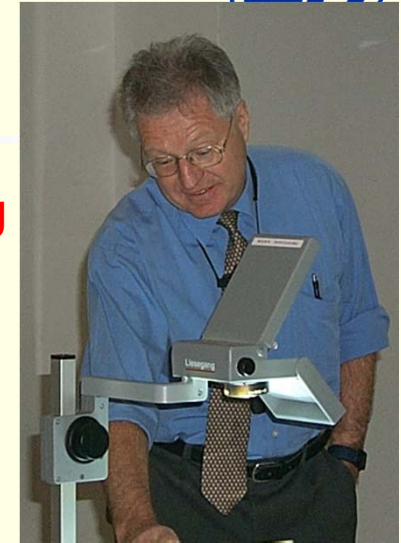
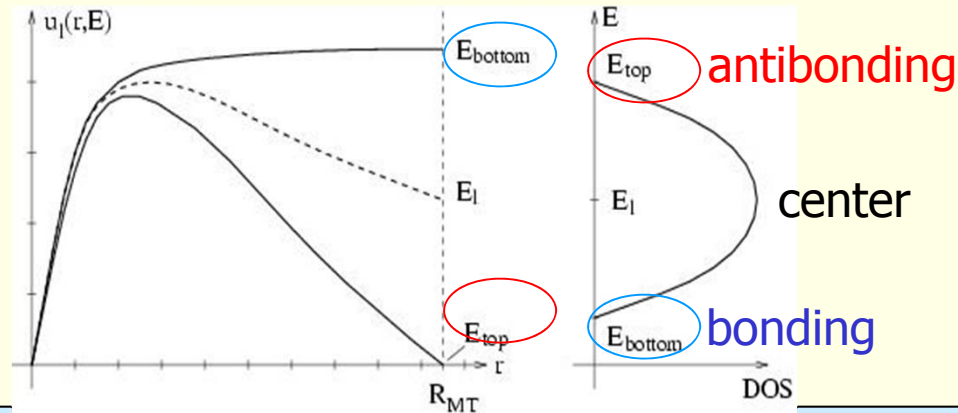
Computationally very demanding
"Exact" solution for a given (spherical) potential!



Linearization of energy dependence

LAPW suggested by

O.K.Andersen,
Phys.Rev. B 12, 3060
(1975)



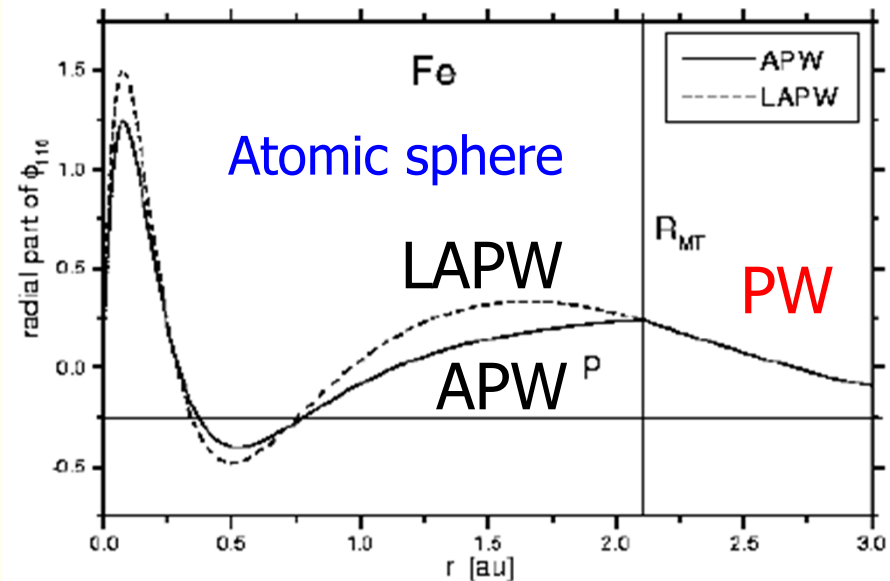
$$\Phi_{k_n} = \sum_{\ell m} [A_{\ell m}(k_n) u_{\ell}(E_{\ell}, r) + B_{\ell m}(k_n) \dot{u}_{\ell}(E_{\ell}, r)] Y_{\ell m}(\hat{r})$$

expand u_l at **fixed energy E_l** and
add $\dot{u}_l = \partial u_l / \partial \varepsilon$

A_{lm}^k, B_{lm}^k : join **PWs** in
value and slope

→ General eigenvalue problem
(diagonalization)

→ additional constraint requires
more **PWs** than APW





Problems of the LAPW method



		Atomic number																					
		Symbol																					
		Atomic weight																					
		Metal										Semimetal						Nonmetal					
1	1	1	2											13	14	15	16	17	18				
1	H	2	He											5	6	7	8	9	10				
	1.008		4.003											10.81	12.01	14.01	16.00	19.00	20.18				
2	3	4											13	14	15	16	17	18					
2	Li	Be											Al	Si	P	S	Cl	Ar					
	6.941	9.012											26.98	28.09	30.97	32.07	35.45	39.95					
3	11	12								8	9	10	11	12	13	14	15	16	17	18			
3	Na	Mg								Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr			
	22.99	24.31								55.85	58.93	58.69	63.55	65.39	69.72	72.61	74.92	78.96	79.90	83.80			
4	19	20								26	27	28	29	30	31	32	33	34	35	36			
4	K	Ca								Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	I	Xe			
	39.10	40.08								101.1	102.9	106.4	107.9	112.4	114.8	118.7	121.8	127.6	126.9	131.3			
5	37	38								44	45	46	47	48	49	50	51	52	53	54			
5	Rb	Sr								Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po	At	Rn			
	85.47	87.62								190.2	192.2	195.1	197.0	200.6	204.4	207.2	209.0	209.0	210.0	222.0			
6	55	56								76	77	78	79	80	81	82	83	84	85	86			
6	Cs	Ba								Hs	Mt	Uun	Uuu	Uub	Uut	Uuq	Uup	Uuh	Uus	Uuo			
	132.9	137.3								265.1	268	269	272	277		289		289		293			
7	87	88								108	109	110	111	112	113	114	115	116	117	118			
7	Fr	Ra								La	Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb
	223.0	226.0								138.9	140.1	140.9	144.2	146.9	150.4	152.0	157.3	158.9	162.5	164.9	167.3	168.9	173.0
										89	90	91	92	93	94	95	96	97	98	99	100	101	102
										Ac	Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No
										227.0	232.0	231.0	238.0	237.0	244.1	243.1	247.1	247.1	251.1	252.0	257.1	258.1	259.1

(c)1998
Kromer Paul



Problems with semi-core states



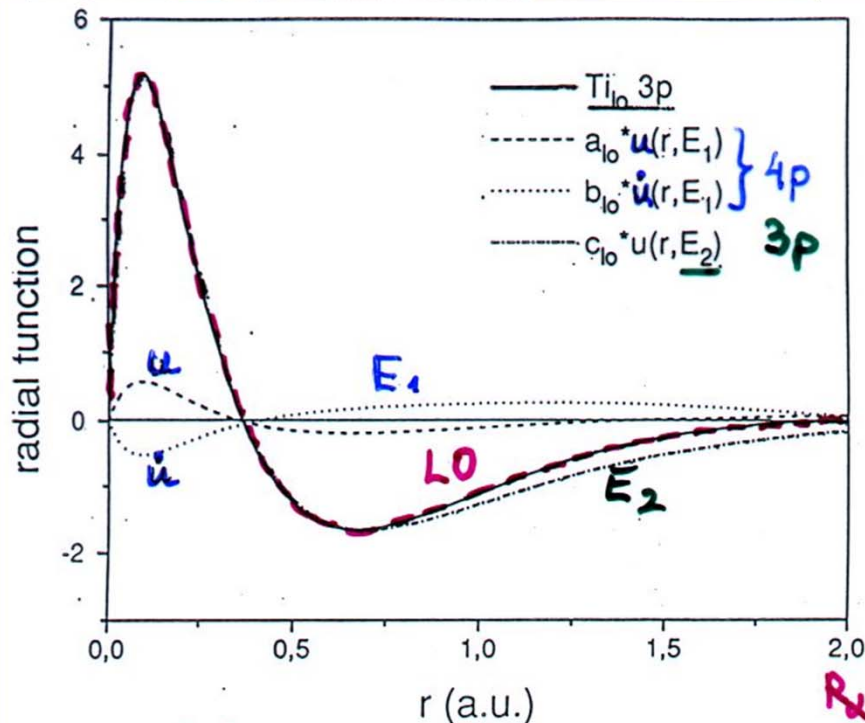
Extending the basis: Local orbitals (LO)



$$\Phi_{LO} = [A_{lm} u_l^{E_1} + B_{lm} \dot{u}_l^{E_1} + C_{lm} u_l^{E_2}] Y_{lm}(\hat{r})$$

■ LO ↑ 4p ↑ 3p

- *is confined to an atomic sphere*
- *has zero value and slope at R*
- *can treat two principal QN n for each azimuthal QN ℓ (3p and 4p)*
- *corresponding states are strictly orthogonal (no "ghostbands")*
- *tail of semi-core states can be represented by plane waves*
- *only slight increase of basis set (matrix size)*



D.J.Singh,
Phys.Rev. B 43 6388 (1991)



New ideas from Uppsala and Washington



E.Sjöstedt, L.Nordström, D.J.Singh,
An alternative way of linearizing the augmented plane wave method,
Solid State Commun. 114, 15 (2000)

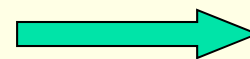
- Use **APW**, but at **fixed E** , (superior PW convergence)
- **Linearize** with **additional lo** (add a few basis functions)

$$\Phi_{k_n} = \sum_{\ell m} A_{\ell m}(k_n) u_{\ell}(E_{\ell}, r) Y_{\ell m}(\hat{r})$$

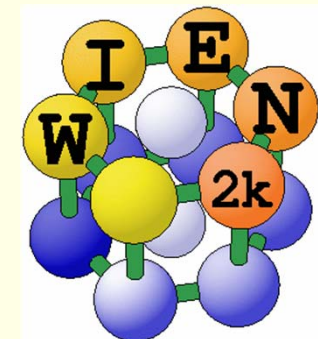
$$\Phi_{lo} = [A_{\ell m} u_{\ell}^{E_1} + B_{\ell m} \dot{u}_{\ell}^{E_1}] Y_{\ell m}(\hat{r})$$

optimal solution: mixed basis

- use APW+lo for states which are difficult to converge:
(f or d- states, atoms with small spheres)
- use LAPW+LO for all other atoms and ℓ



basis for





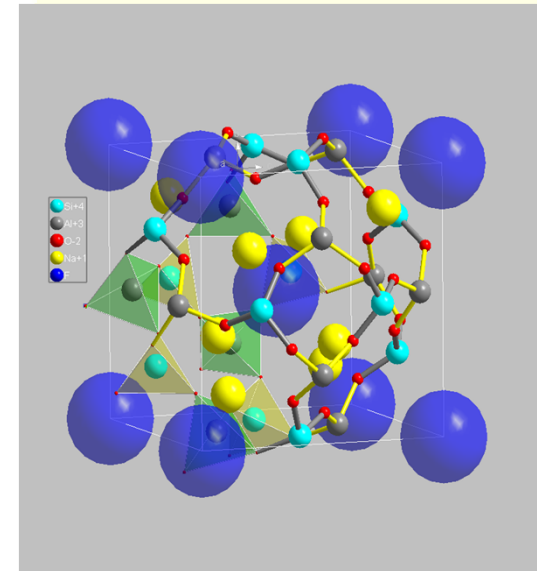
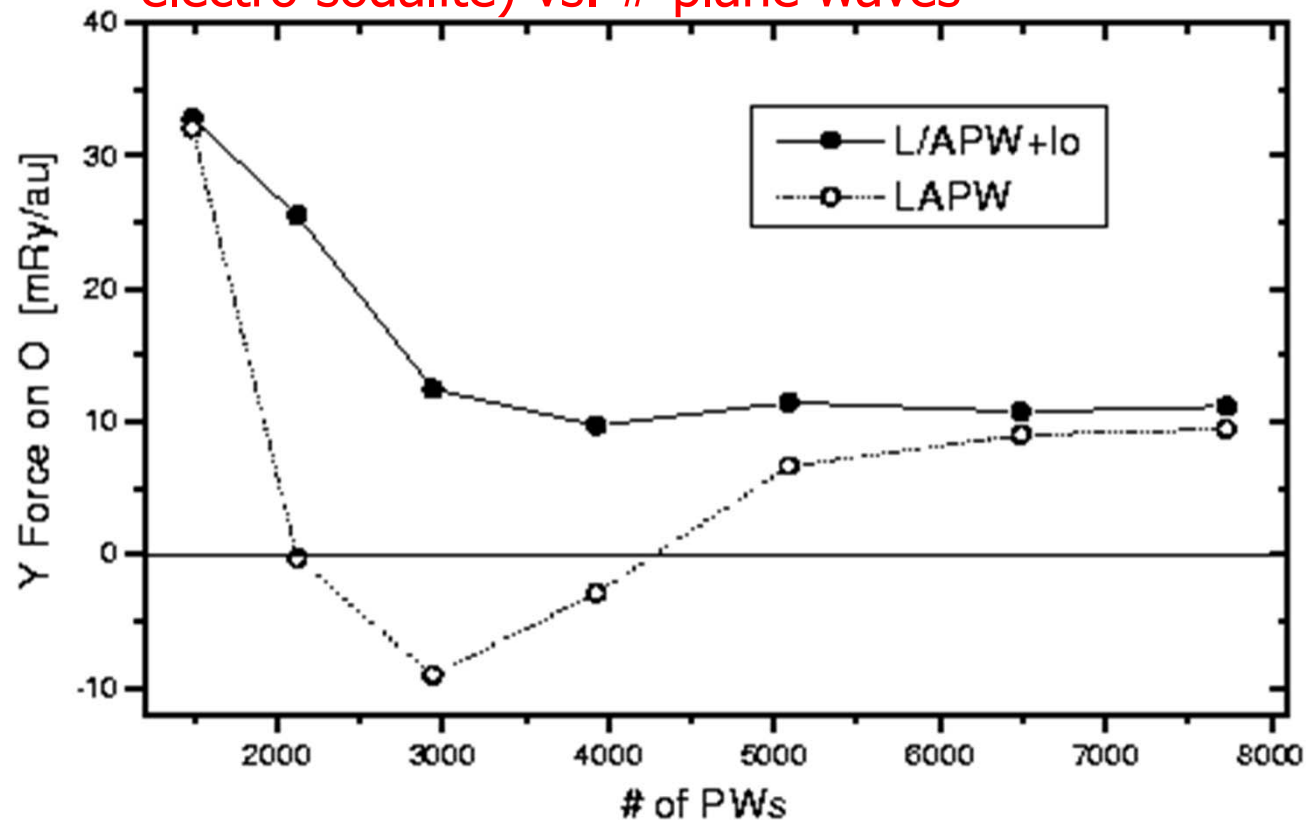
Improved convergence of APW+lo



K.Schwarz, P.Blaha, G.K.H.Madsen,
Comp.Phys.Commun. **147**, 71-76 (2002)

- changes sign and converges slowly in **LAPW**
- better convergence in **APW+lo**

Force (F_y) on oxygen in SES (sodium electro sodalite) vs. # plane waves

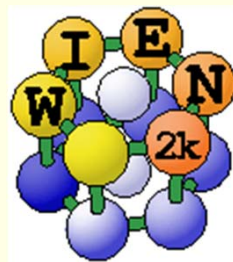




APW based schemes



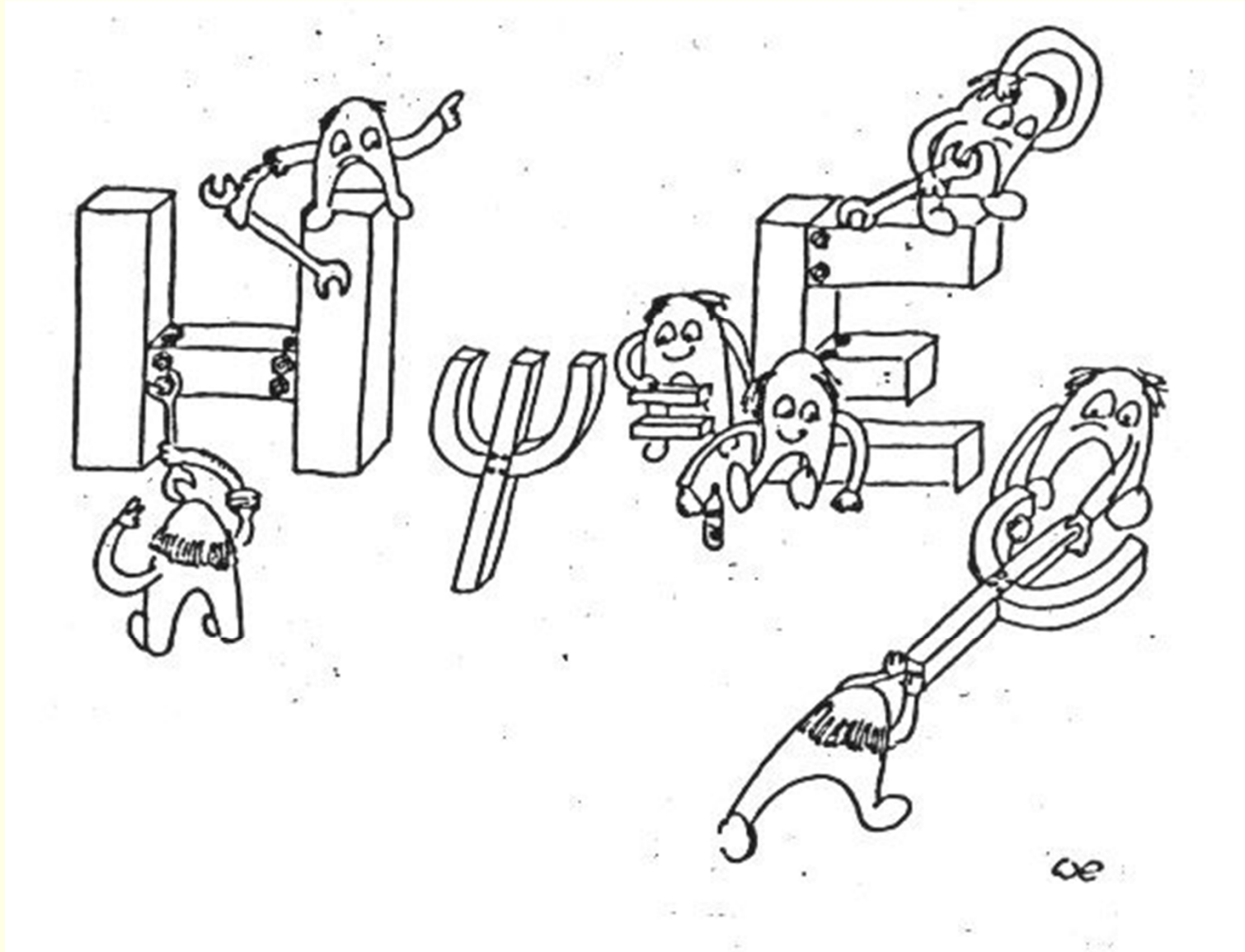
- **APW (J.C.Slater 1937)**
 - *Non-linear eigenvalue problem*
 - *Computationally very demanding*
- **LAPW (O.K.Andersen 1975)**
 - *Generalized eigenvalue problem*
 - *Full-potential (A. Freeman et al.)*
- **Local orbitals (D.J.Singh 1991)**
 - *treatment of semi-core states (avoids ghostbands)*
- **APW+lo (E.Sjöstedt, L.Nordström, D.J.Singh 2000)**
 - *Efficiency of APW + convenience of LAPW*
 - *Basis for*



K.Schwarz, P.Blaha, G.K.H.Madsen,
Comp.Phys.Commun. **147**, 71-76 (2002)

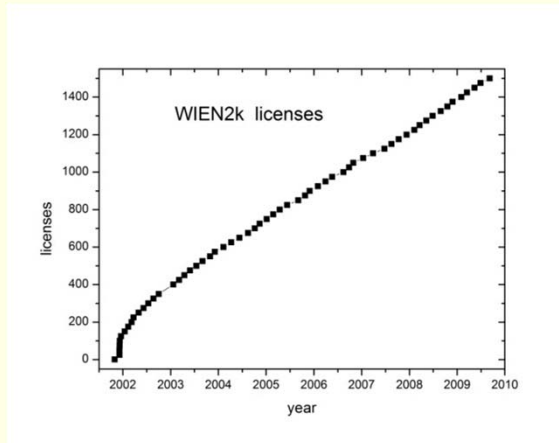
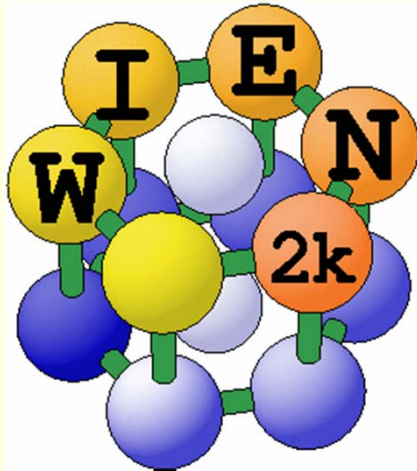


Quantum mechanics at work





WIEN2k software package



WIEN2k: ~1700 groups
mailinglist: 1800 users

**An Augmented Plane Wave Plus Local
Orbital
Program for Calculating Crystal Properties**

**Peter Blaha
Karlheinz Schwarz
Georg Madsen
Dieter Kvasnicka
Joachim Luitz**

November 2001
Vienna, AUSTRIA
Vienna University of Technology

<http://www.wien2k.at>

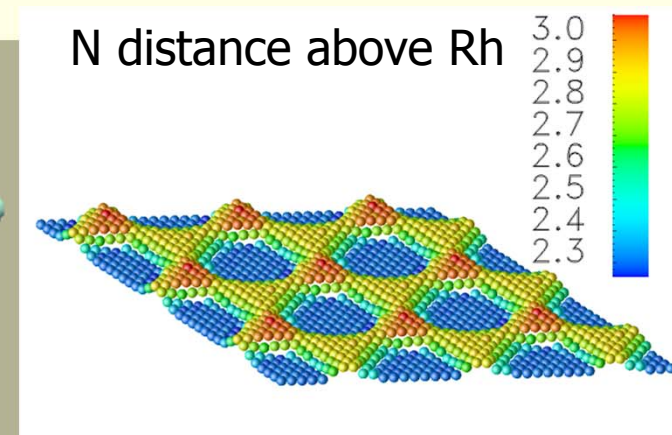
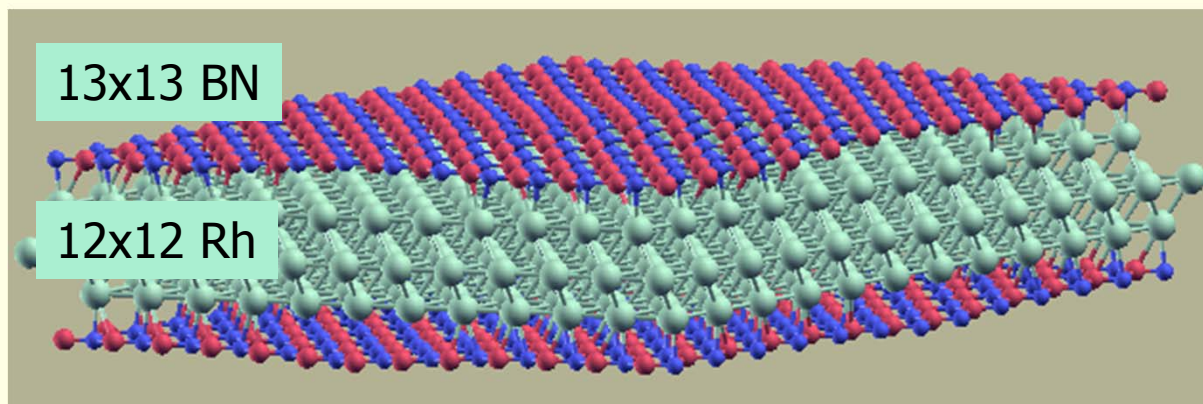


General remarks on WIEN2k



- WIEN2k consists of many independent F90 programs, which are linked together via C-shell scripts (needs Unix/Linux)
- real/complex version (inversion)
- k-point parallel on clusters with common NFS (slow network)
- MPI/Scalapack parallelization for bigger cases (>50 atoms) and fast network

h-BN/Rh(111) nanomesh: **1108** atoms on 64-512 cpus





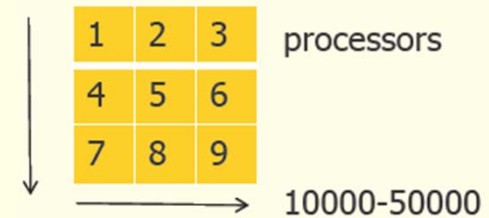
mpi-parallel version: (R.Laskowski)



■ setup and solution of generalized eigenvalue problem: $HC = ESC$

■ *large problems: diagonalization of matrices 100000x100000*

- ~ 100 GB memory (impossible to store on "one" computer)
- distribute matrices onto many nodes



■ *diagonalization*

- Scalapack is 2 times slower than LAPACK
- takes 10 times more time than setup

➡ *bottleneck*

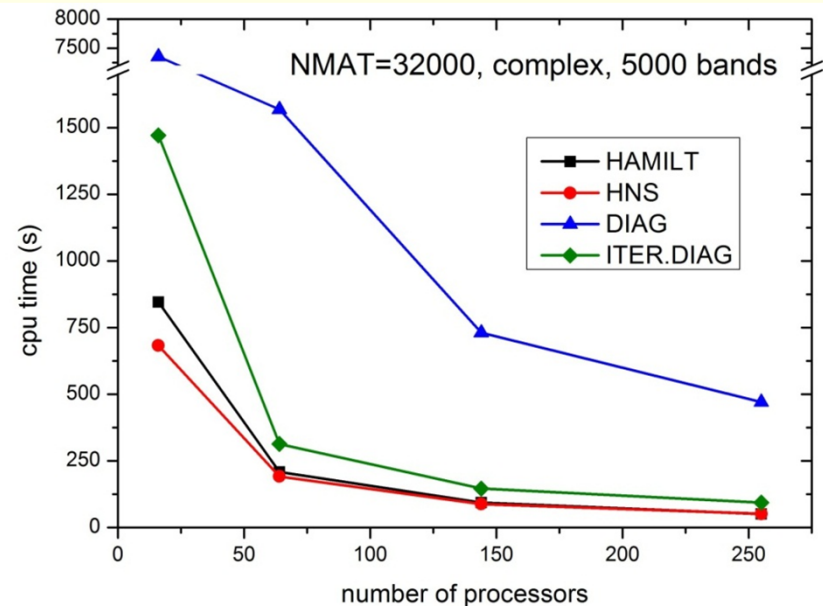
- iterative diagonalization 10x faster
- good scaling requires fast network

■ *matrix setup*

- almost 100% parallel efficiency

Note: 1% sequential code

➡ *50% efficiency on 100 nodes*





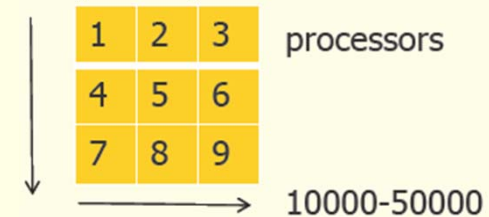
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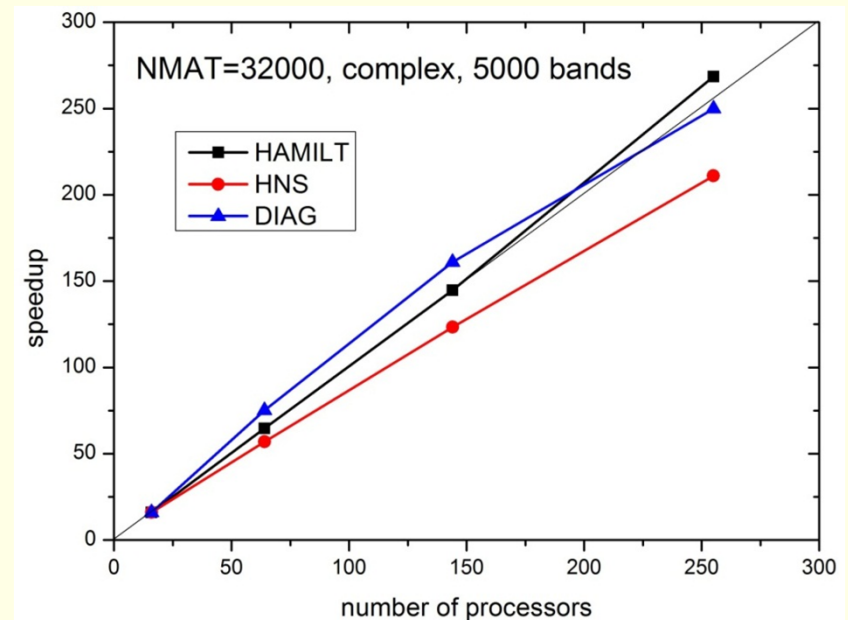
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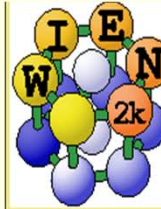




w2web GUI (graphical user interface)



- **Structure generator**
 - *spacegroup selection*
 - *import cif file*
- **step by step initialization**
 - *symmetry detection*
 - *automatic input generation*
- **SCF calculations**
 - *Magnetism (spin-polarization)*
 - *Spin-orbit coupling*
 - *Forces (automatic geometry optimization)*
- **Guided Tasks**
 - *Energy band structure*
 - *DOS*
 - *Electron density*
 - *X-ray spectra*
 - *Optics*



Execution >>

StructGen™
initialize calc.
run SCF
single prog.
optimize(V,c/a)
mini. positions

Utils. >>

Tasks >>

Files >>

struct file(s)
input files
output files
SCF files

Session Mgmt. >>

change session
change dir
change info

Configuration

Usersguide

html-Version
pdf-Version

Idea and realization
by

Session: TiC

/area51/pblaha/lapw/2005-june/TiC

StructGen™

You have to click "Save Structure" for changes to take effect!

Save Structure

Title: TiC

Lattice:

Type: F

P
F
B
CXY
CYZ
CXZ
R
H
1_P1

Spacegroups from
Bilbao Cryst Server

Lattice parameters in Å

a=4.328000038 b=4.328000038 c=4.328000038
 $\alpha=90.000000$ $\beta=90.000000$ $\gamma=90.000000$

Inequivalent Atoms: 2

Atom 1: Ti Z=22.0 RMT=2.0000 remove atom

Pos 1: x=0.00000000 y=0.00000000 z=0.00000000 remove
add position

Atom 2: C Z=6.0 RMT=1.9000 remove atom

Pos 1: x=0.50000000 y=0.50000000 z=0.50000000 remove
add position

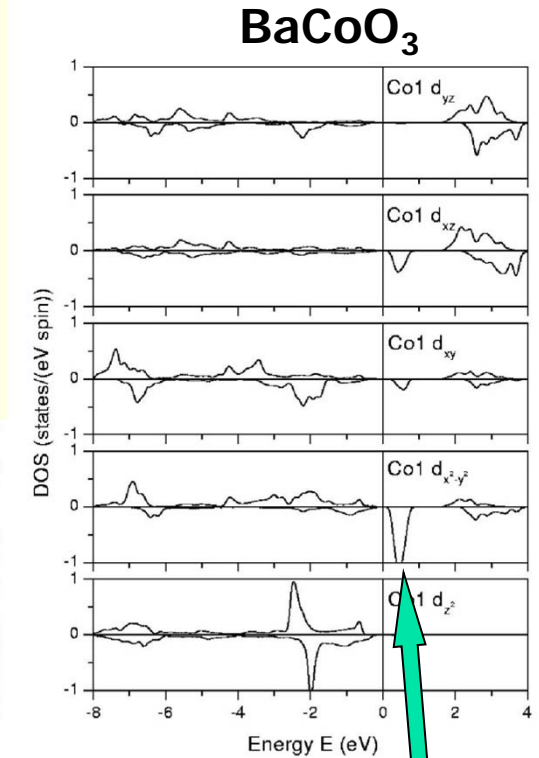
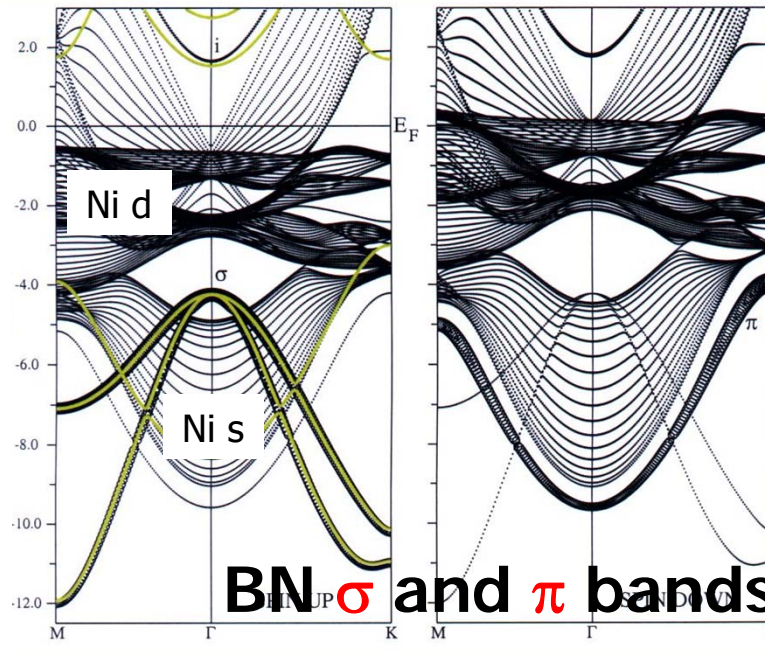
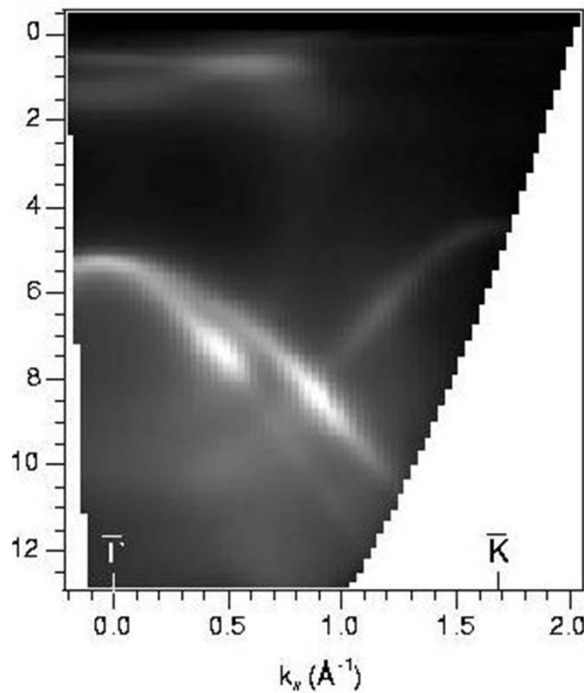


Properties with WIEN2k - I



- **DFT:** LDA, various GGAs; meta-GGA, LDA+U; Hybrid-DFT for „correlated electrons“)
- **Energy bands**
 - *classification of irreducible representations*
 - *'character-plot' (emphasize a certain band-character)*
- **Density of states**
 - *including partial DOS with l and m-character*

h-BN/Ni(111): σ and π bands



$d-x^2-y^2$

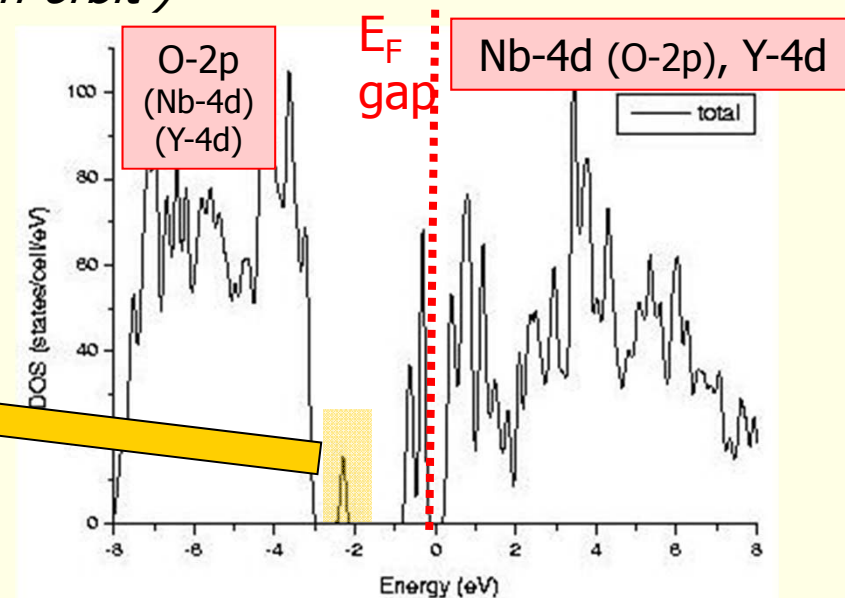
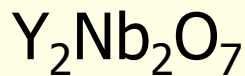
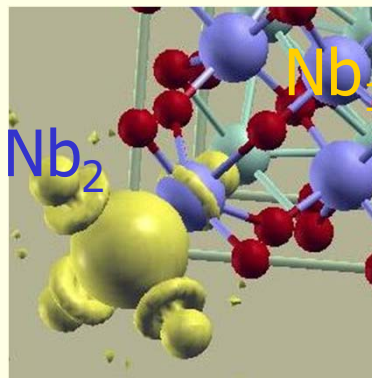


Properties with WIEN2k - II



■ Electron densities, potential

- *total-, valence-, difference-, spin-densities, ρ of selected states*
- *1-D, 2D- and 3D-plots (Xcrysden)*
- *X-ray structure factors, STM pictures*
- *Bader's atom-in-molecule analysis, atomic basins and charges ($\nabla \rho \cdot \vec{n} = 0$)*
- *spin+orbital magnetic moments (+ spin-orbit)*



■ Hyperfine parameters

- *Isomer shift*
- *Electric field gradients*
- *hyperfine fields (contact + dipolar + orbital contribution)*

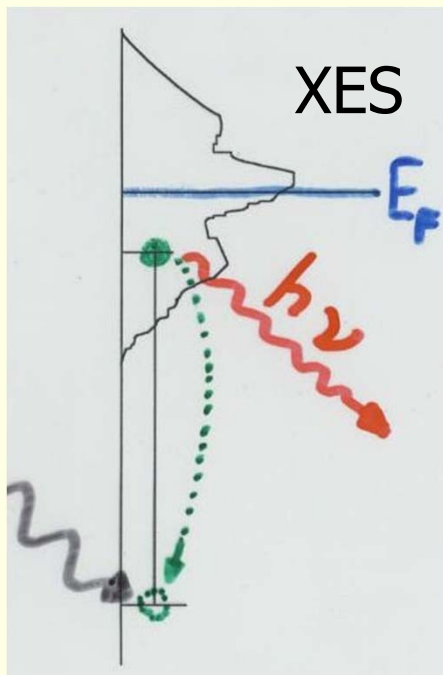


Properties with WIEN2k - III



■ Spectroscopy

- *core levels (with core holes)*
- *X-ray emission, absorption, electron-energy-loss*
 - (core - valence/conduction-band transitions including matrix elements and angular dep.)
 - EELS inclusion of possible non-dipol transittions (momentum transfer)
- *optical properties (dielectric function in RPA, JDOS including momentum matrix elements and Kramers-Kronig)*
- *fermi surface (2D, 3D)*

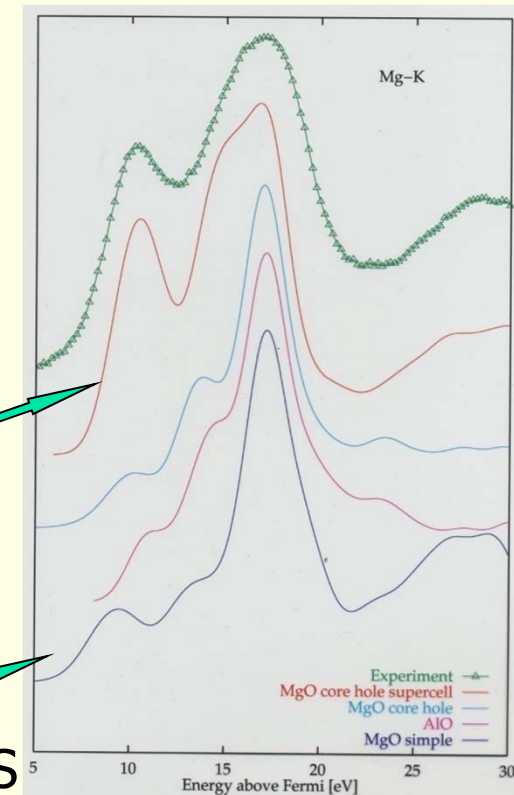


Mg-K XAS

probes empty Mg-p

including a core-hole
in supercell
(Final state rule)

from ground-state DOS





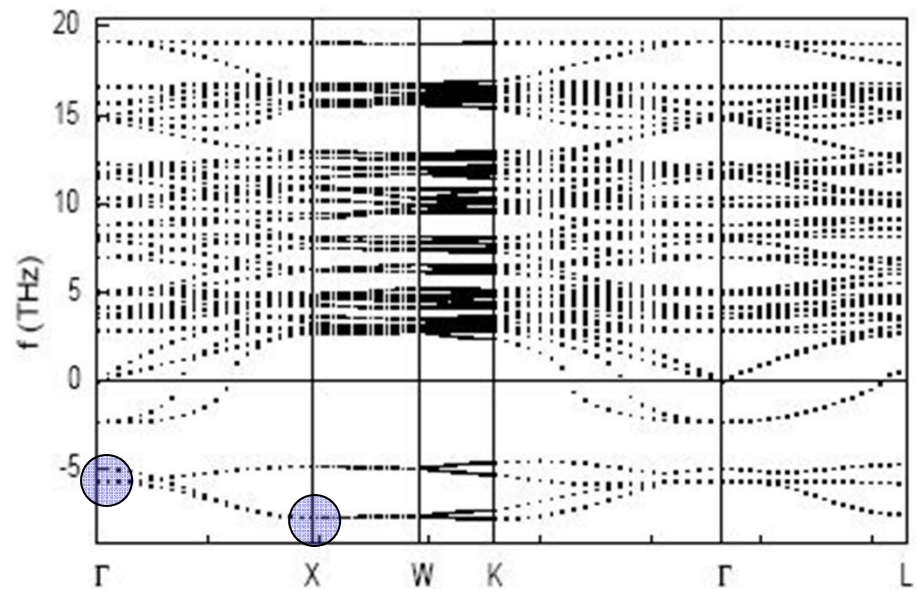
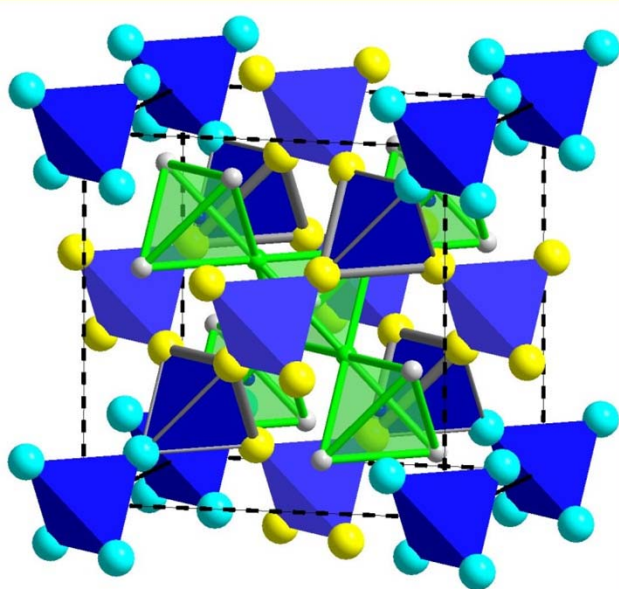
Properties with WIEN2k - IV



■ Total energy and forces

- *optimization of internal coordinates, (damped MD, BROYDEN)*
- *cell parameter only via E_{tot} (no stress tensor)*
- *elastic constants for cubic cells*
- *Phonons via a direct method (based on forces from supercells)*
 - interface to PHONON (K.Parlinski) – bands, DOS, thermodynamics, neutrons

Pyrochlore structure of $Y_2Nb_2O_7$: strong phonon instabilities \rightarrow phase transition





Total energies and atomic forces

(Yu et al.; Kohler et al.)



Total Energy:

- *Electrostatic energy*
- *Kinetic energy*
- *XC-energy*

$$U[\rho] = \frac{1}{2} \int d^3\vec{r} \rho(\vec{r}) V_{es}(\vec{r}) + \frac{1}{2} \sum_{\alpha} Z_{\alpha} V_{es}^{\alpha}(\vec{r})$$

$$T[\rho] = \sum_i n_i \varepsilon_i - \int d^3\vec{r} \rho(\vec{r}) V_{eff}(\vec{r})$$

$$E_{xc}[\rho] = \int d^3\vec{r} \rho(\vec{r}) \varepsilon_{xc}(\vec{r})$$

Force on atom α :

$$\vec{F}^{\alpha} = \frac{-dE_{tot}}{d\vec{R}_{\alpha}} = F_{HF}^{\alpha} + F_{core}^{\alpha} + F_{val}^{\alpha}$$

- *Hellmann-Feynman-force*
- *Pulay corrections*

$$F_{HF}^{\alpha} = Z_{\alpha} \sum_{m=-1}^1 \lim_{r_{\alpha} \rightarrow 0} \frac{V_{1m}^{es}(r_{\alpha})}{r_{\alpha}} \nabla_{\alpha} [r_{\alpha} Y_{1m}(\hat{r})]$$

- *Core*
- *Valence*

$$F_{core}^{\alpha} = - \int \rho_{core}(r) \nabla_{\alpha} V_{eff}(r) d\vec{r}$$

- **expensive, contains a summation of matrix elements over all occupied states** (done only in last scf-iteration)

$$F_{val}^{\alpha} = \int_{\alpha} V_{eff}(r) \nabla_{\alpha} \rho_{val}(r) d\vec{r} + \sum_{k,i} n_i \sum_{K,K'} c_i^*(K') c_i(K) \times$$

$$\left[(K^2 - \varepsilon_i) \oint \phi_{K'}^*(r) \phi_K(r) dS_{\alpha} - i(K - K') \langle \phi_{K'} | H - \varepsilon_i | \phi_K \rangle_{\alpha} \right]$$

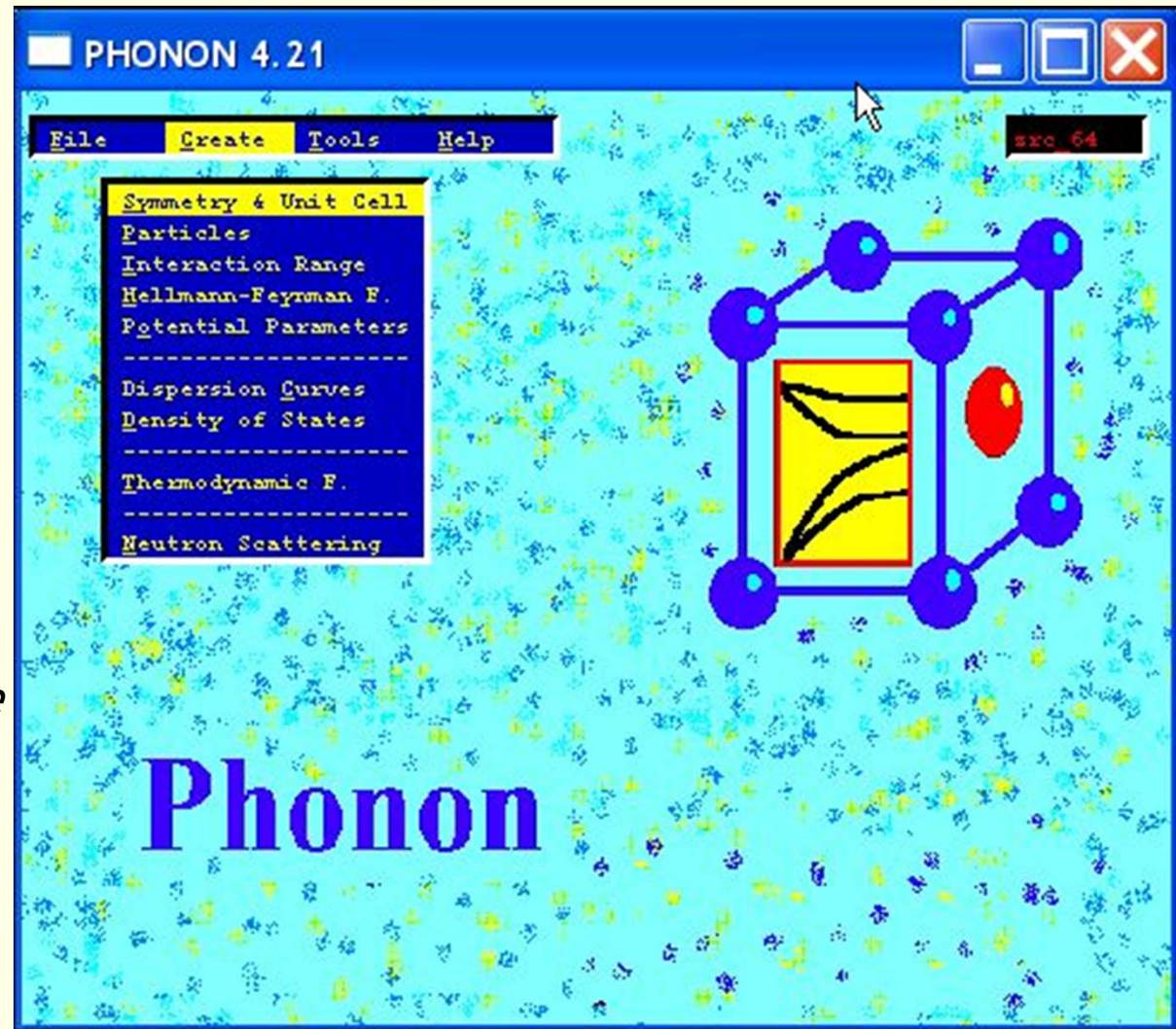


PHONON-I



■ PHONON

- *by K.Parlinski (Crakow)*
- *uses a „direct“ method to calculate Force-constants with the help of an ab initio program*
- *with these Force-constants phonons at arbitrary k-points can be obtained*
- **Define your spacegroup**
- **Define all atoms at previously optimized positions**





PHONON-II



- Define an interaction range (supercell)
 - create *displacement* file
 - transfer *case.d45* to Unix
- Calculate forces for all required displacements
 - *init_phonon_lapw*
 - for each displacement a *case_XX.struct* file is generated in an extra directory
 - runs *nn* and lets you define *RMT* values like:
 - 1.85 1-16



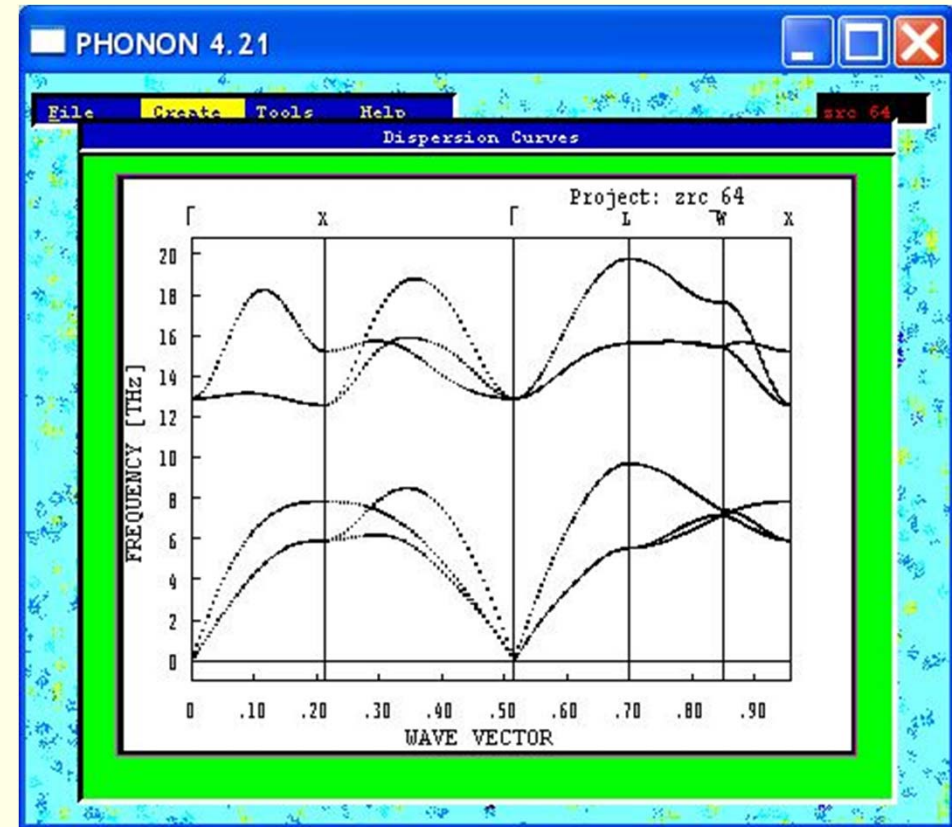
- *init_lapw*: either *without symmetry* (and then copies this setup to all *case_XX*) or *with symmetry* (must run *init_lapw* for all *case_XX*) (Do NOT use *SGROUP*)
- *run_phonon*: *run_lapw -fc 0.1 -i 40* for each *case_XX*



PHONON-III



- **analyze_phonon_lapw**
 - reads the *forces* of the *scf* runs
 - generates „*Hellman-Feynman*“ file *case.dat* and a „*symmetrized HF-file case.dsy* (when you have displacements in both directions)
 - check quality of forces:
 - $\sum F_x$ should be small (0)
 - $\text{abs}(F_x)$ should be similar for \pm -displacements
- **Import HF files to PHONON**
- **Calculate phonons**

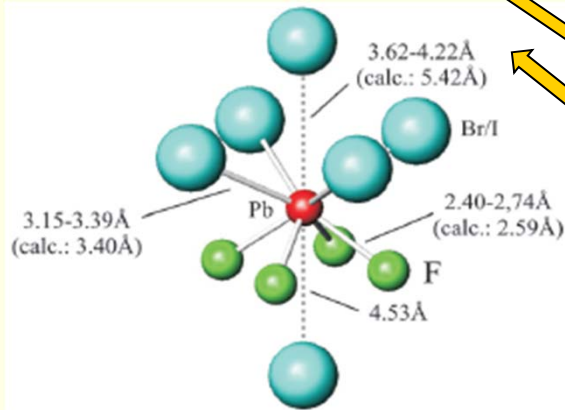




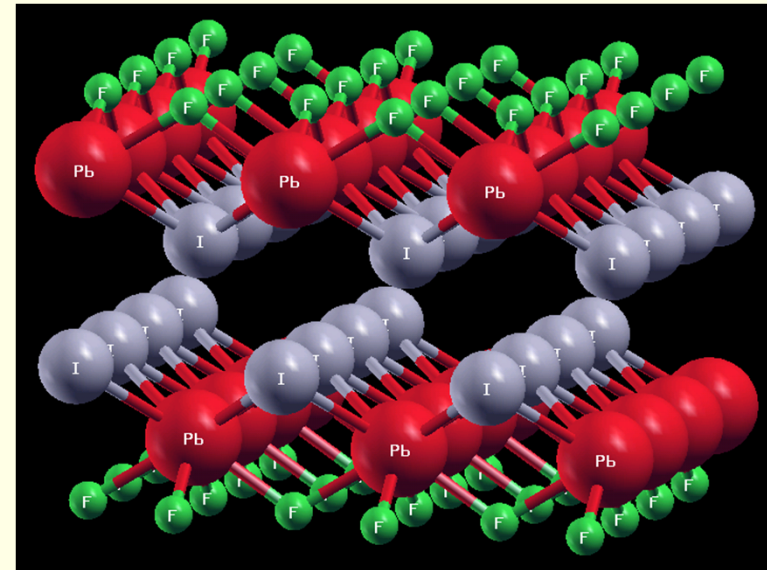
Γ - Phonons in matlockite PbFI



	a	c	c/a	z_1/c	z_{Pb}/c
Calc.	4.227	10.02	2.371	0.690 (0.659)	0.149 (0.167)
Expt	4.2374	8.800	2.077	0.663	0.164



I-I interaction



Symmetry	Atoms	Calc. ^a	Calc. ^b	Expt
$E_g(R)$	$Pb_1(x, y), Pb_2(-x, -y), I_1(-x, -y), I_2(x, y)$	36	41	36
$E_u(I)$	$Pb_1(-x, -y), Pb_2(-x, -y), F_1(x, y), F_2(x, y), I_1(x, y), I_2(x, y)$	35	47	50, 62 [16]
$E_g(R)$	$Pb_1(-x, -y), Pb_2(x, y), F_1(x, -y), F_2(-x, y), I_1(-x, -y), I_2(x, y)$	40	64	61
$A_{2u}(I)$	$Pb_1(-z), Pb_2(-z), I_1(z), I_2(z)$	79	71	
$A_{1g}(R)$	$Pb_1(z), Pb_2(-z), I_1(-z), I_2(z)$	61	73	67
$A_{1g}(R)$	$Pb_1(z), Pb_2(-z), I_1(z), I_2(-z)$	108	109	105
$E_u(I)$	$F_1(x, y), F_2(x, y)$	141	150	142, 154 [16]
$B_{1g}(R)$	$F_1(-z), F_2(z)$	194	207	206
$E_g(R)$	$F_1(-x, -y), F_2(x, y)$	212	217	
$A_{2u}(I)$	$F_1(z), F_2(z)$	274	259	318, 332 [16]

^a Calculated at the theoretical lattice parameters (see table 4).

^b Calculated at the experimental lattice parameters.

H. Hageman et al., J. Phys.: Cond. Mat. 19 (2007)

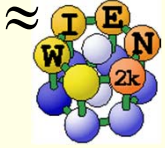


Ferroelectricity in Aurivillius phases

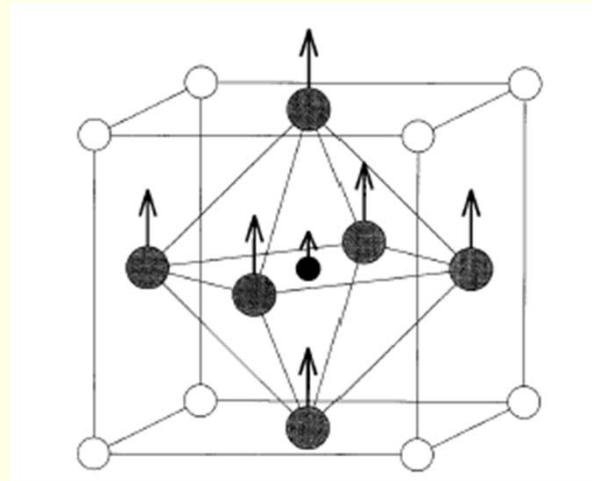


- *** Bilbao: J. Manuel Perez-Mato, M. Aroyo**
- **Universidad del País Vasco**
- *** Vienna: P. Blaha, K. Schwarz,**
- **J. Schweifer**
- *** Cracow: K. Parlinski**

- **J.M. Perez-Mato et al. PRB, 70, 214111**



Ferroelectric Perovskites: PbTiO_3



PbTiO_3

- Ferroelectric PT due to symmetry break at T_c :
cubic ---- tetragonal
Pm-3m ----- P4mm
- A **single** (degenerate) **normal mode** is responsible for the PT
- Structure in Ferroelectric Phase:

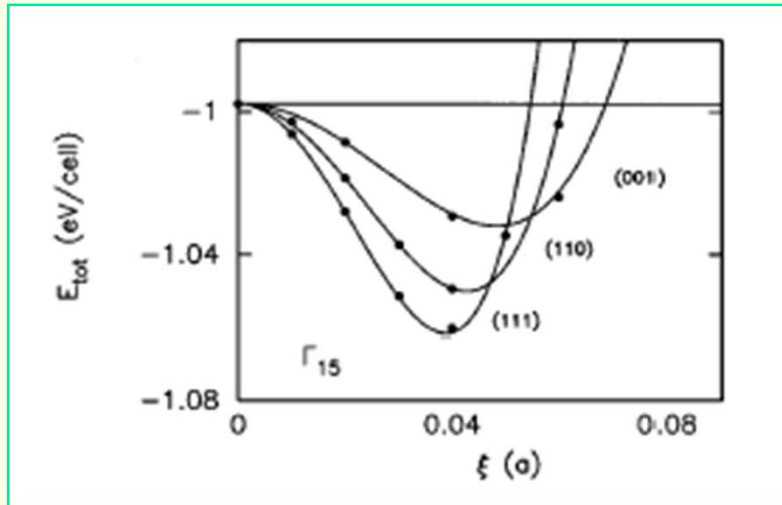
high-symmetry structure + frozen polar mode



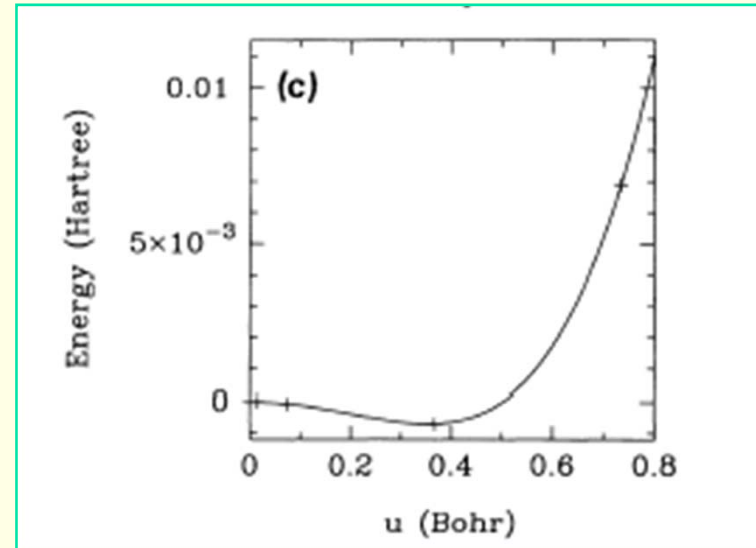
Ab-initio “prediction” of the ferroelectric instability



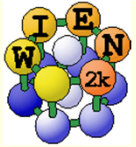
PbTiO₃



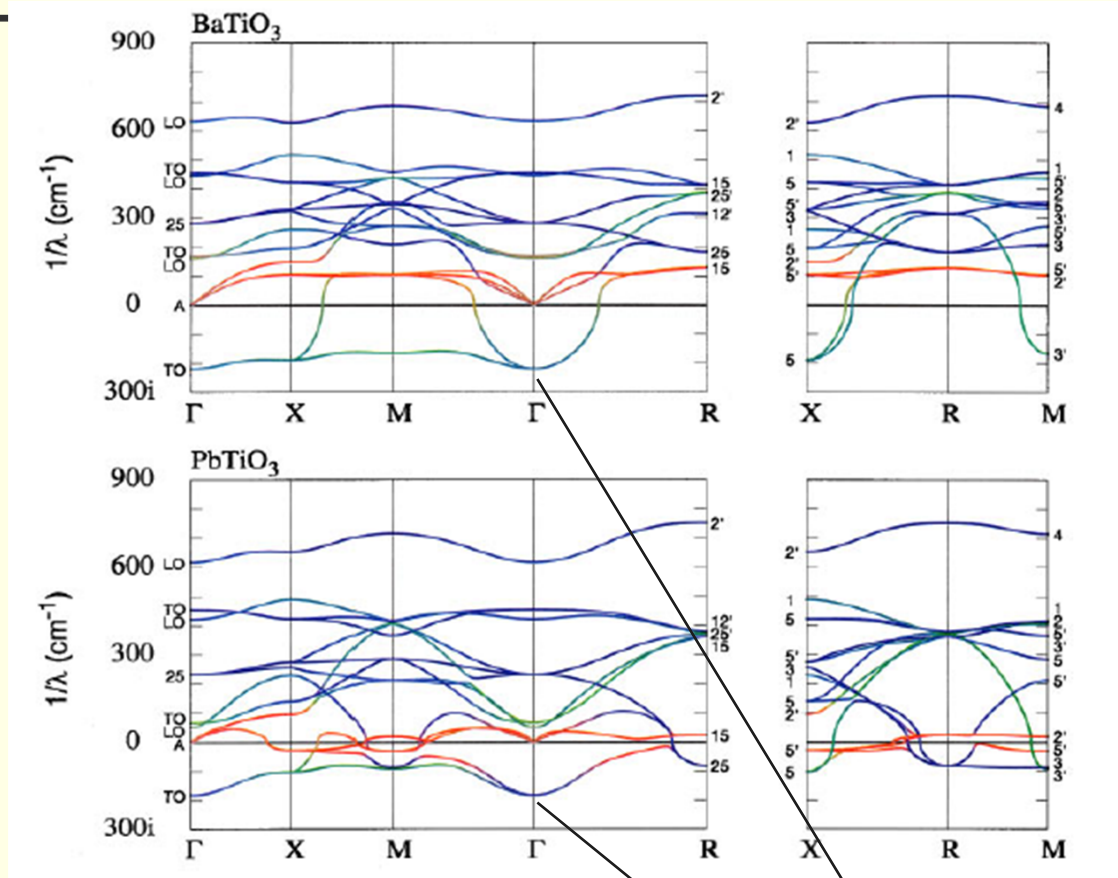
Waghmare&Rabe 1997



King-Smith&Vanderbilt 1994



Ab-initio Phonon Branches

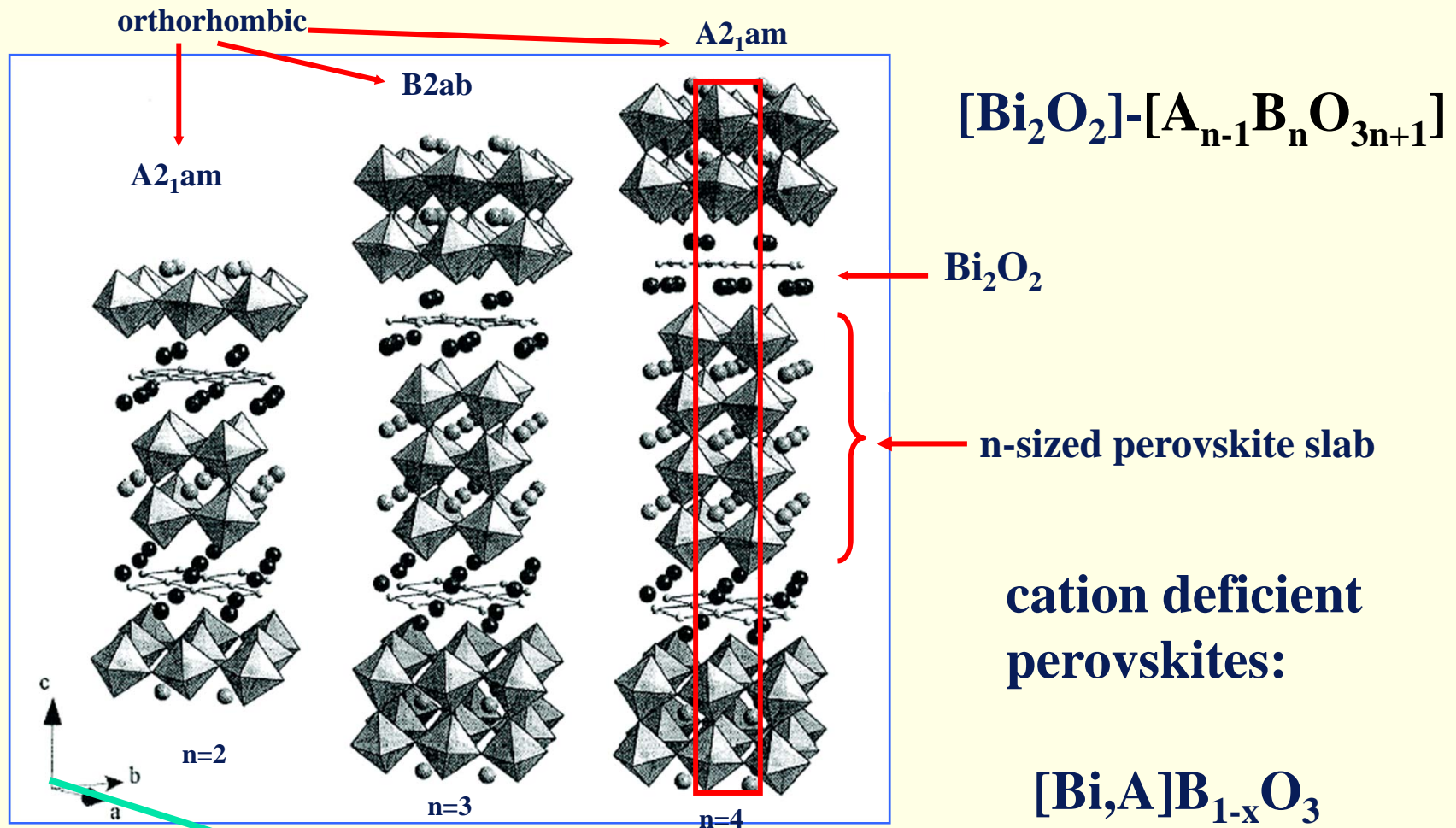


Ghosez et al. 1999

Polar unstable mode



The Aurivillius Compounds

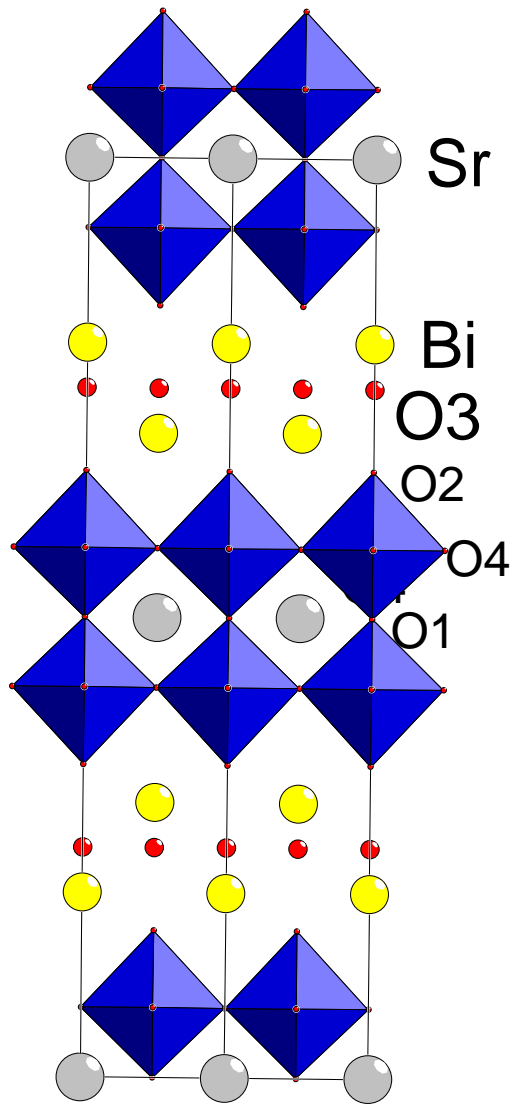


Ps

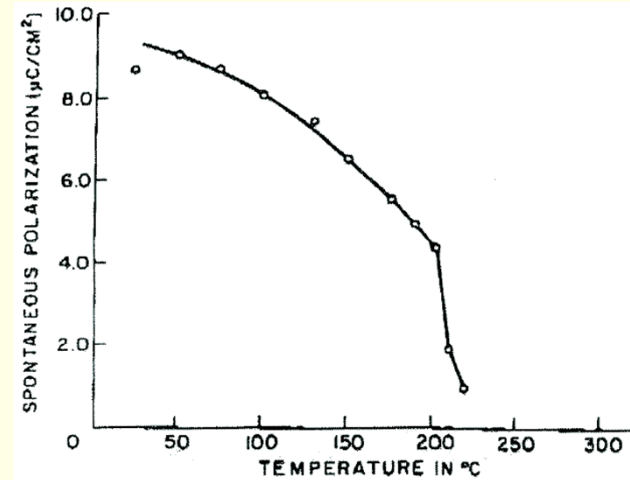
Dipl. Thesis -S. Borg 2001



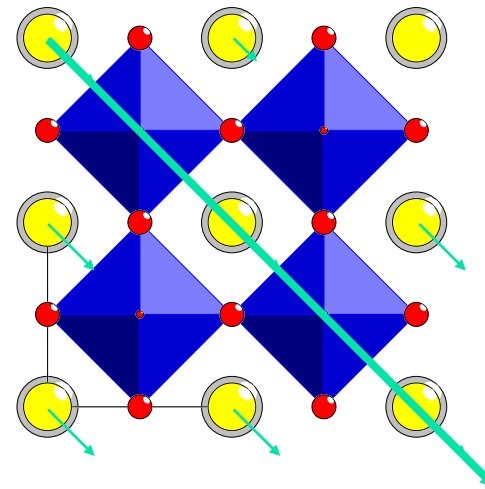
Bi₂SrTa₂O₉ - SBT



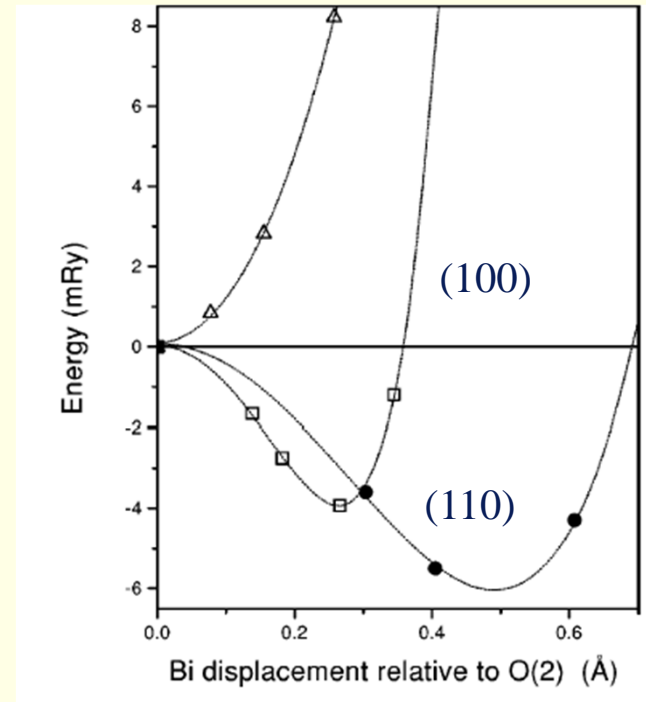
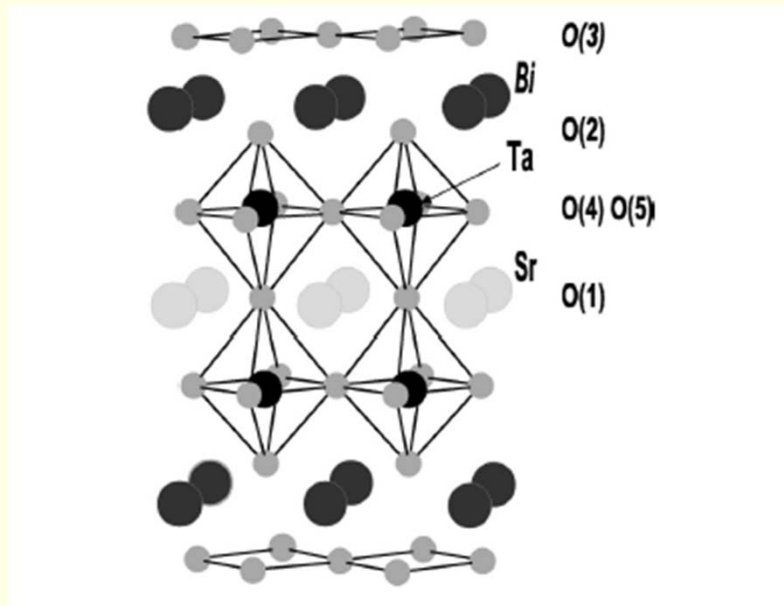
Spontaneous Polarization



polar E_u mode (deg. 2)



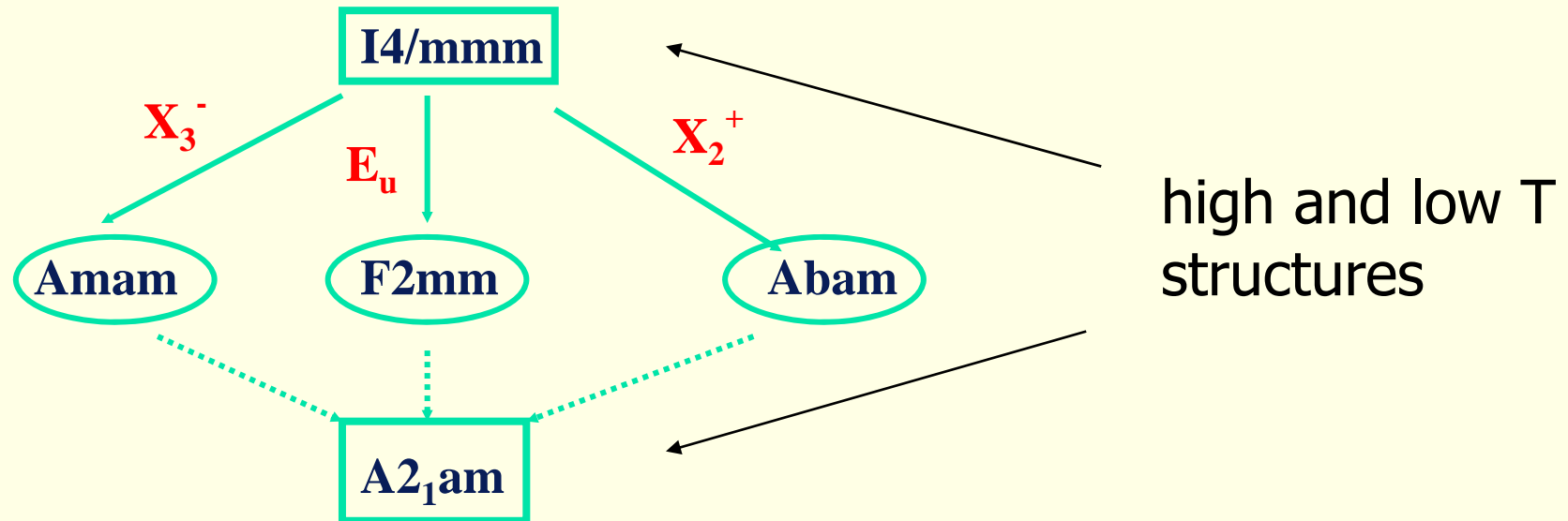
Stachiotti et al. 2000



- **Unstable E_u polar mode**
- **Strong contribution of Bi displacement :
Bi-O(2) hybridization**



SBT – An Usual Ferroelectric? **NO !**

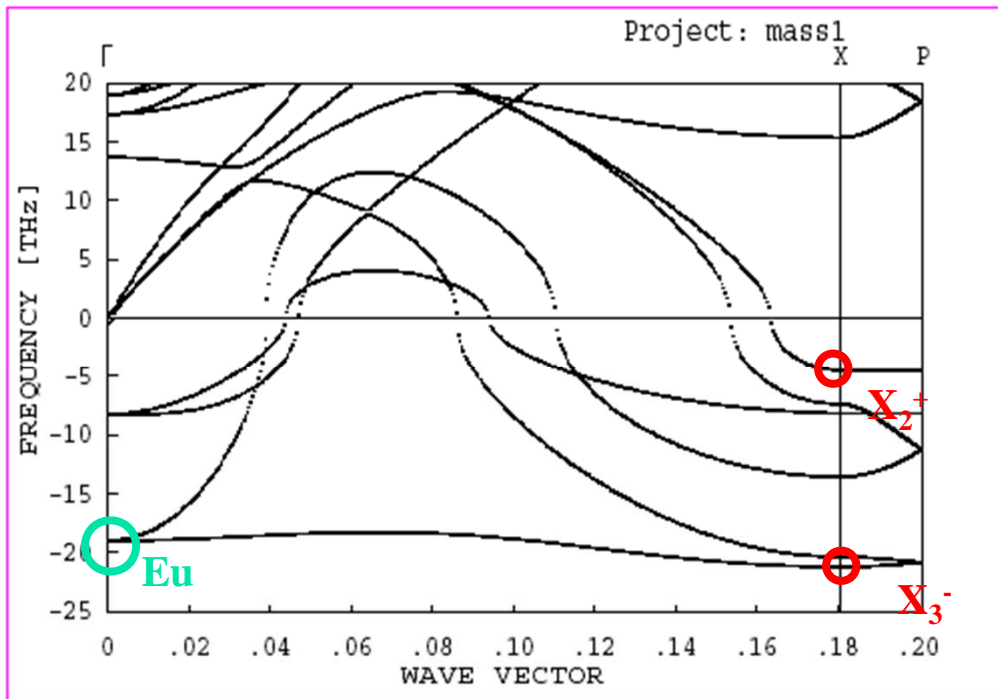
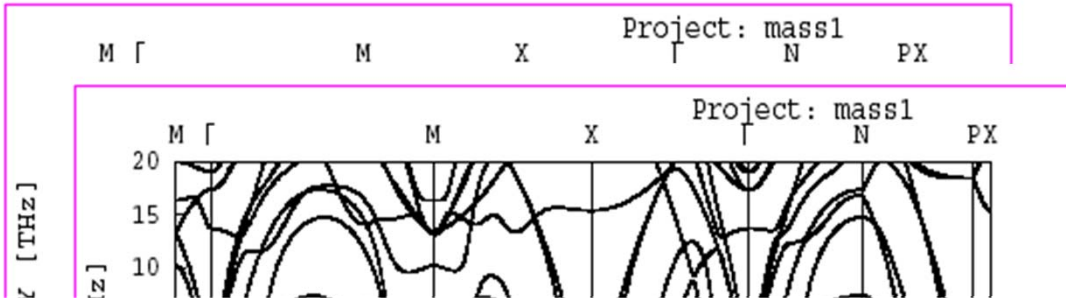


From symmetry analysis (group/ subgroup relations) the **E_u mode alone cannot explain** the complete phase transition

Ferroelectric Phase = $E_u + X_3^- + X_2^+$ mode

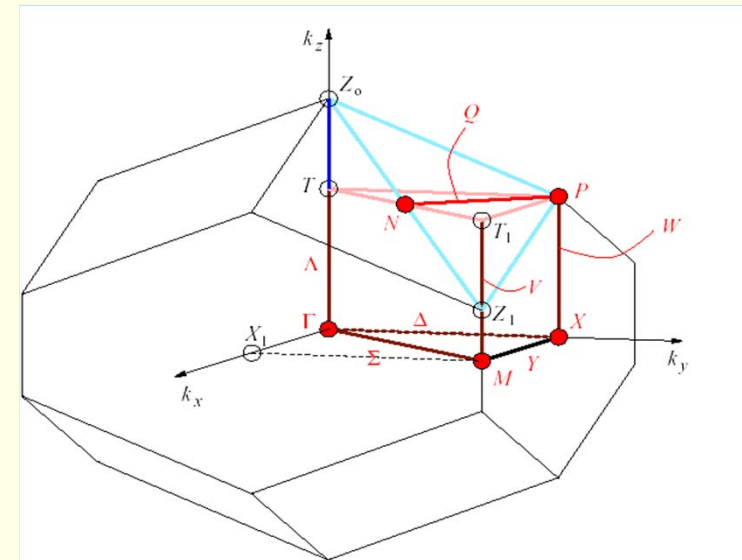


Phonons in SBT



SBT

CALCULATED "PHONON" BRANCHES





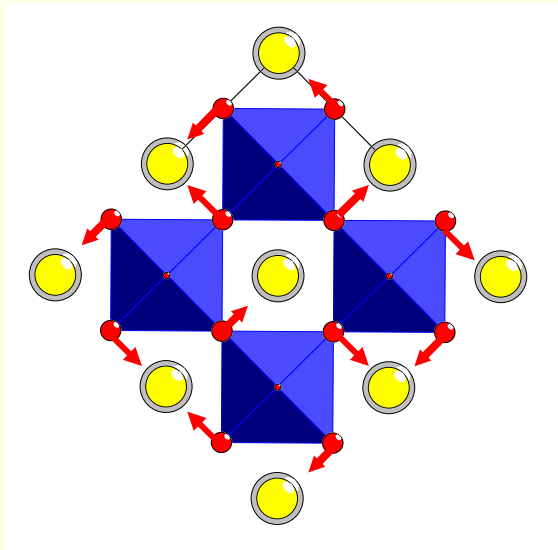
Ferroelectric Phase = $E_u + X_3^- + X_2^+$ mode

Theoretical E_u and X_3^- modes agree well with experimental modes

**BUT ! The experimental X_2^+ mode does not match
the theoretical soft X_2^+ mode**



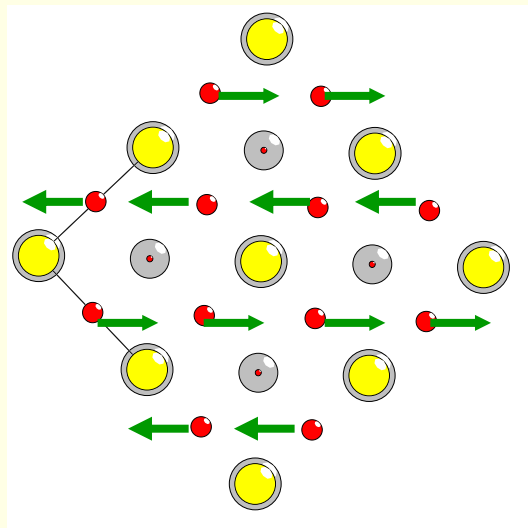
A hard X_2^+ Modes agrees with experiment



calculated X_2^+ soft-mode

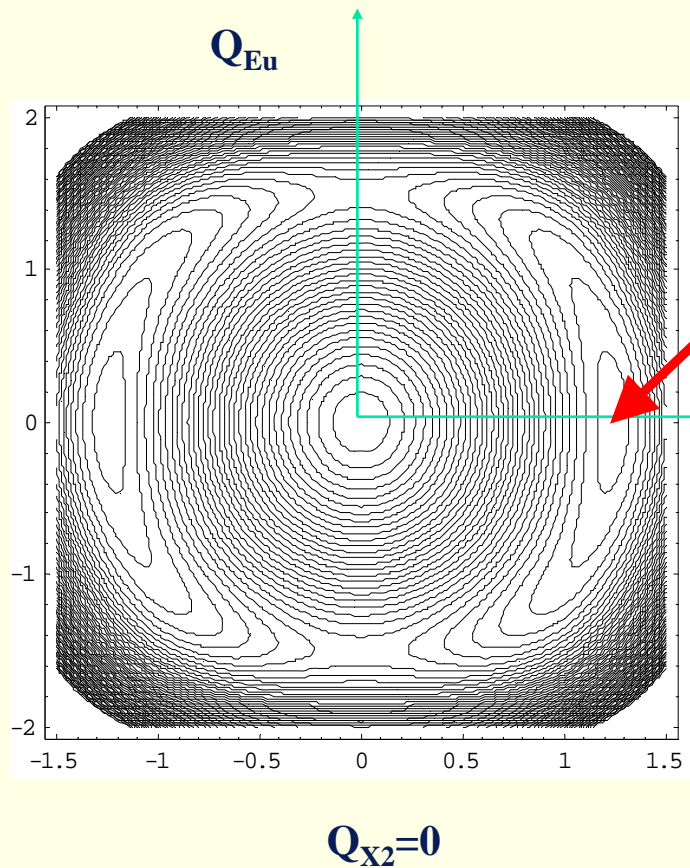
“Part 1”

Two independent normal-modes



“Part 2”

second (hard) mode X_2^+
coincides with exp.



Predicted Ground State:

Only mode X_3^- frozen !

Space group Amam

Essential reason:

**Strong biquadratic coupling
penalizes “mixed” states**

Something missing?

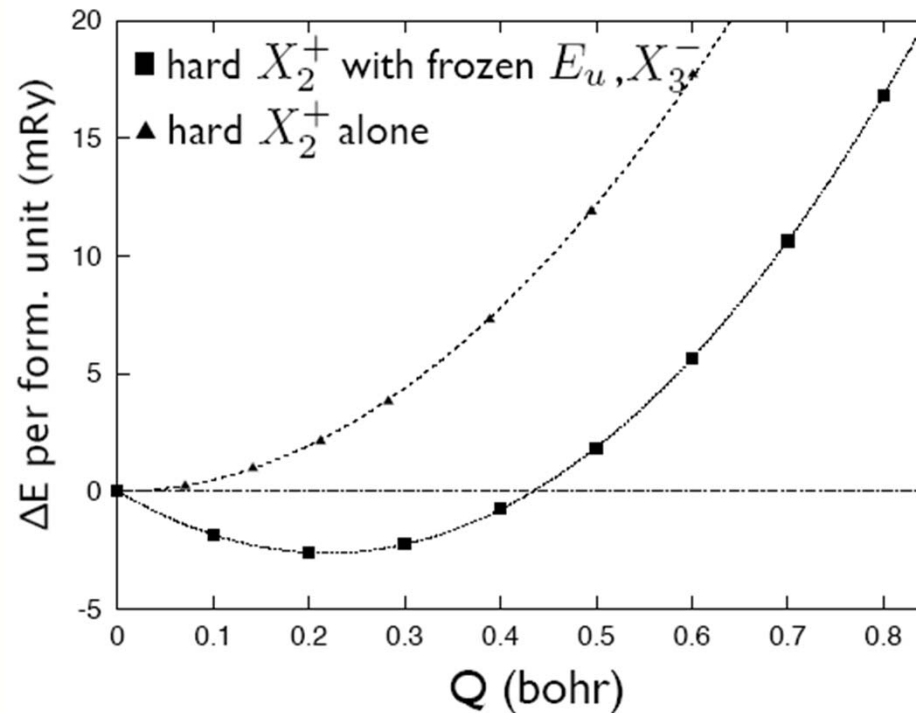
•coupling with X_2^+



Coupling with X_2^+



- Coupling with **soft** X_2^+ mode relatively weak !
- **Strong renormalization** of **hard (second)** X_2^+ mode



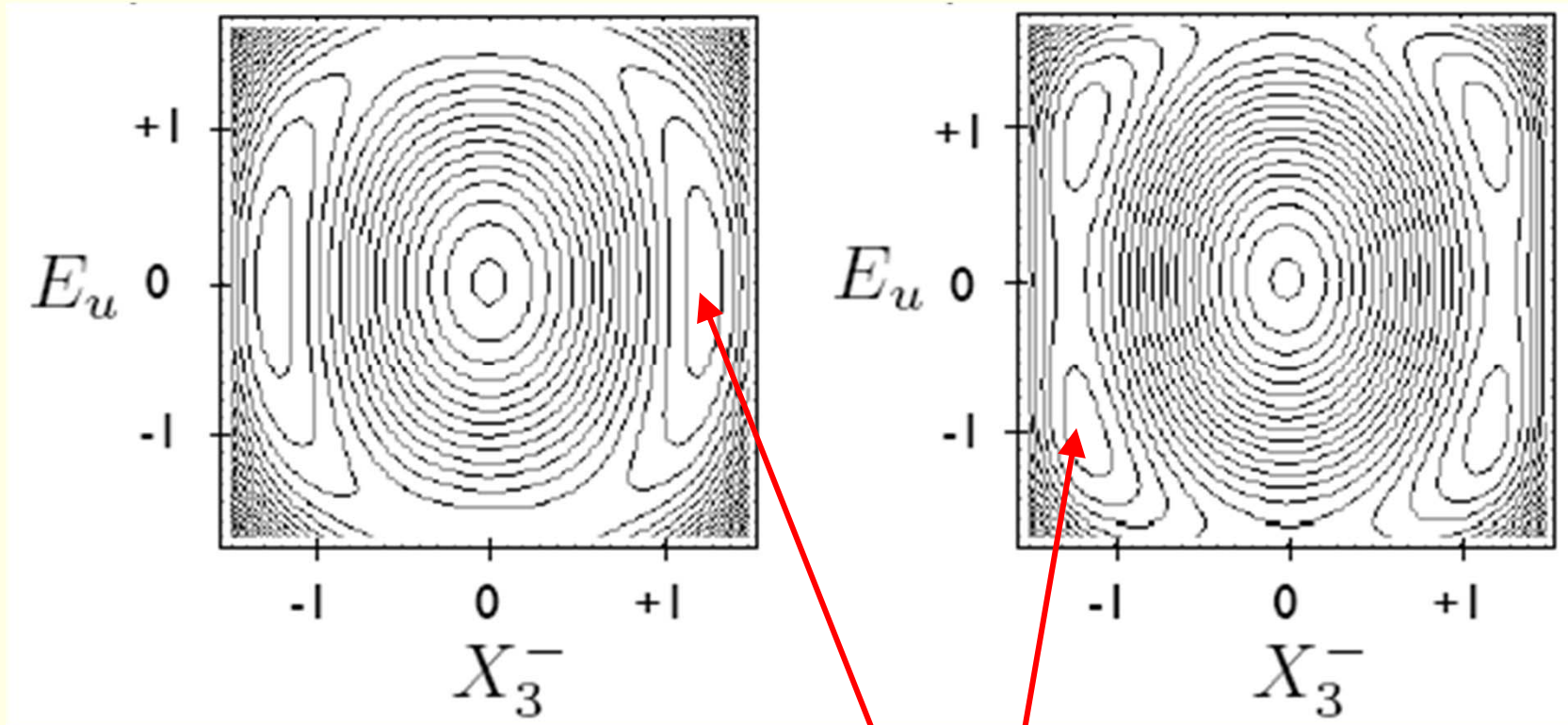


Energy landscape in SBT



including only **soft** X_2^+ mode

with additional **hard** X_2^+ mode



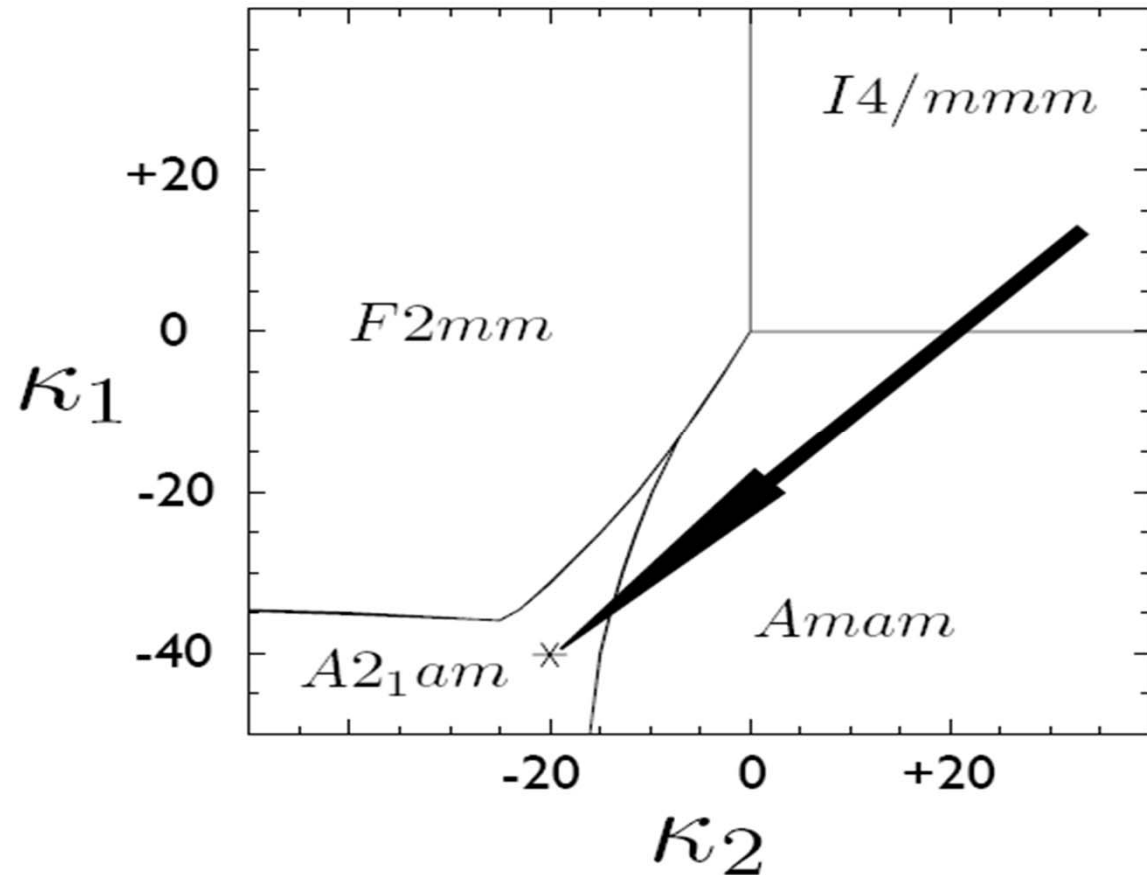
only with the **additional hard** X_2^+ mode the experimentally observed combination of **3 different modes** can be established



Phase diagram for $\text{Bi}_2\text{SrTa}_2\text{O}_9$ - SBT



- Finite temperature renormalization of the $T=0$ energy map
- Landau theory suggests linear T -variation of the quadratic stiffness coefficients κ_{Eu} and κ_{X3^-}



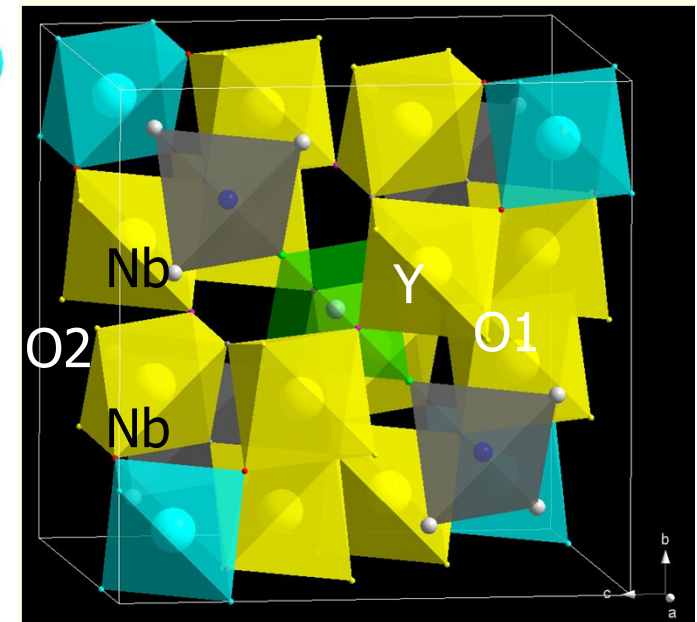
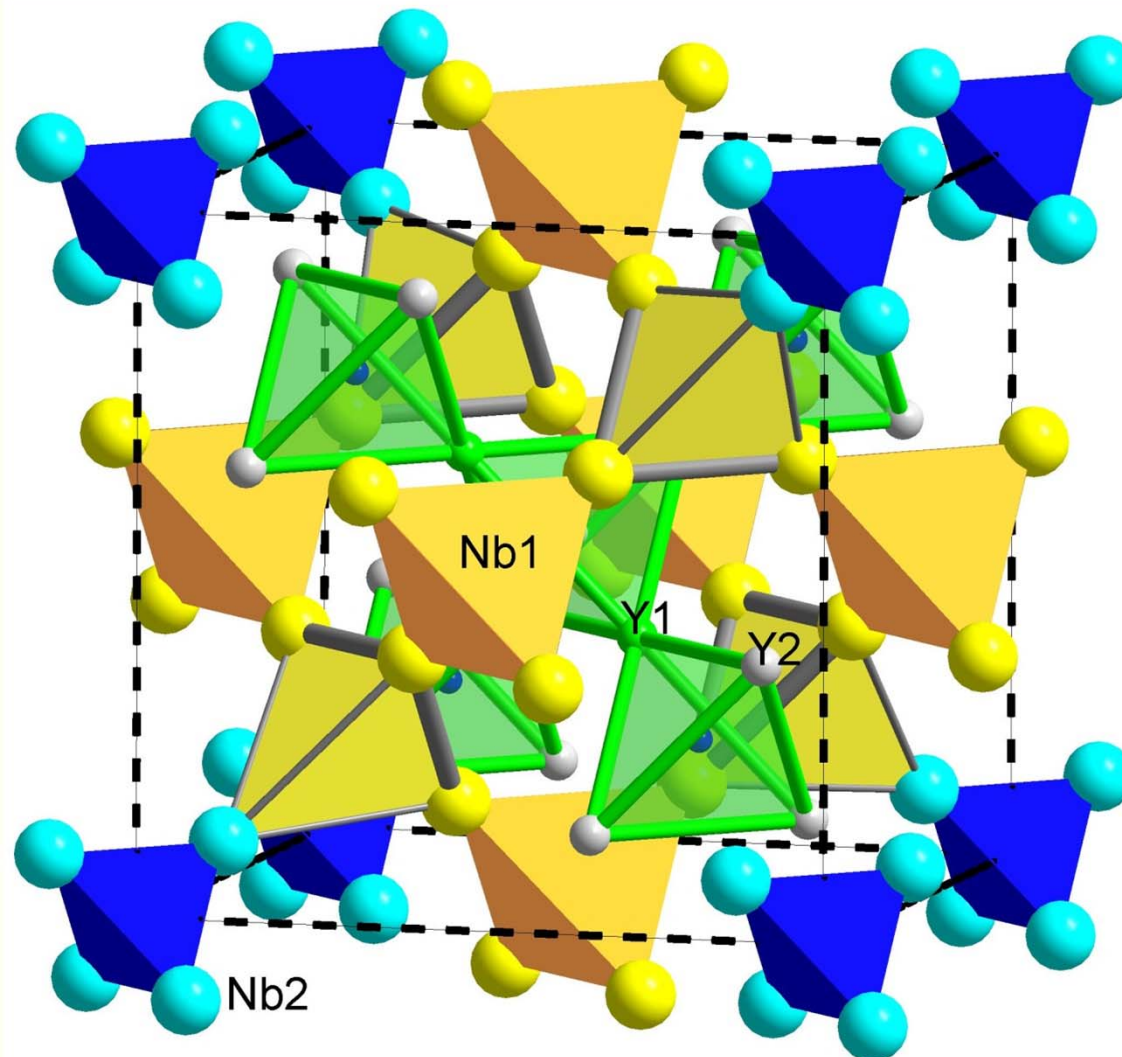
The topology of this phase diagram predicts **two second order** phase transitions and implies the existence of an **intermediate phase** of *Amam* symmetry. A **single first order** PT is impossible.



Pyrochlore $Y_2Nb_2O_7$



Insulating and non-magnetic 4d TM-oxide



Metal Sublattice:
Corner-shared
tetrahedral network

P.Blaha, D.Singh, K.Schwarz,
PRL 93, 216403 (2004)

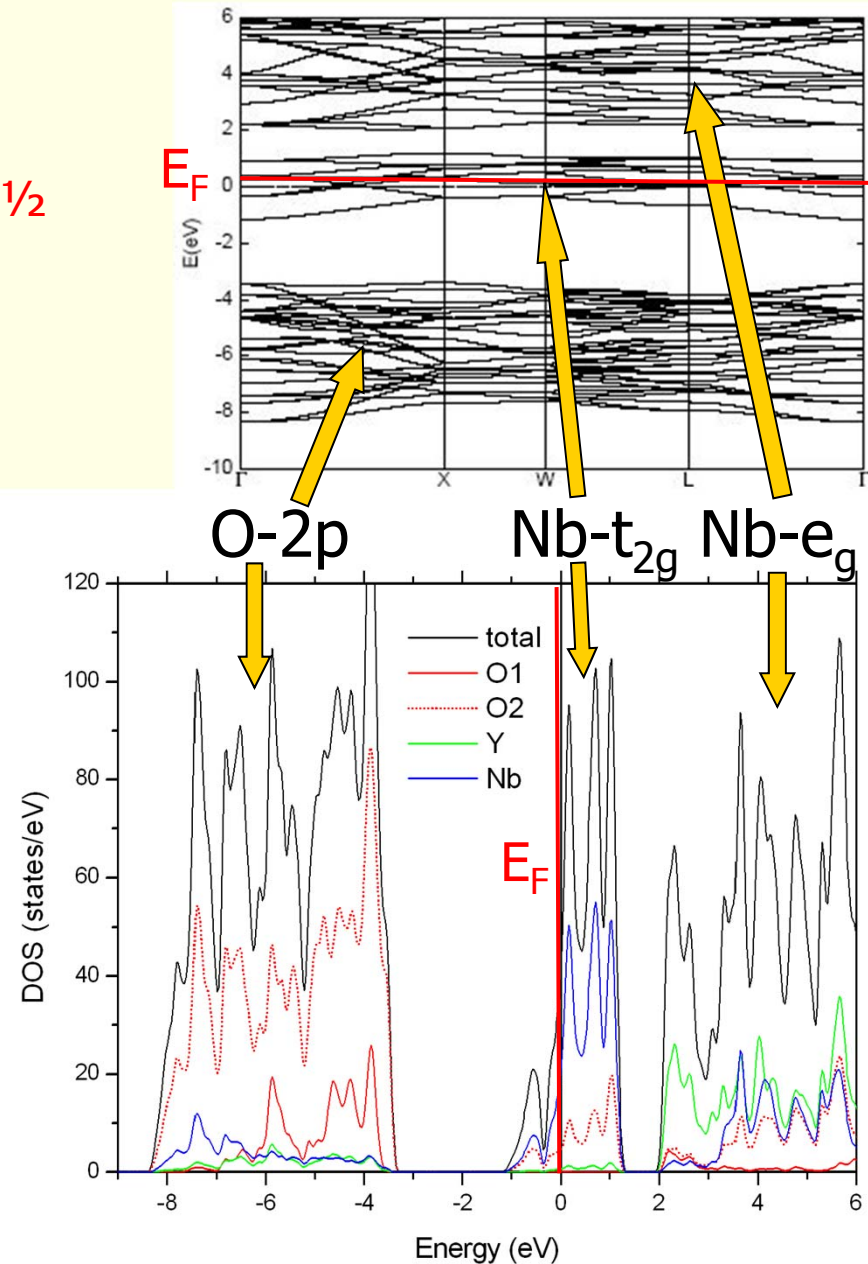


First theoretical results:



- Ionic model: $Y_2^{3+}Nb_2^{4+}O_7^{2-}$ $Nb^{4+}: 4d^1$
- → metallic or localized system with spin $1/2$ (neither one observed in exp.)
- LDA gives nonmagnetic metallic ground-state with conventional t_{2g} - e_g splitting due to the octahedral crystal field of the oxygen atoms.

“degenerate” t_{2g} states are only partly filled.





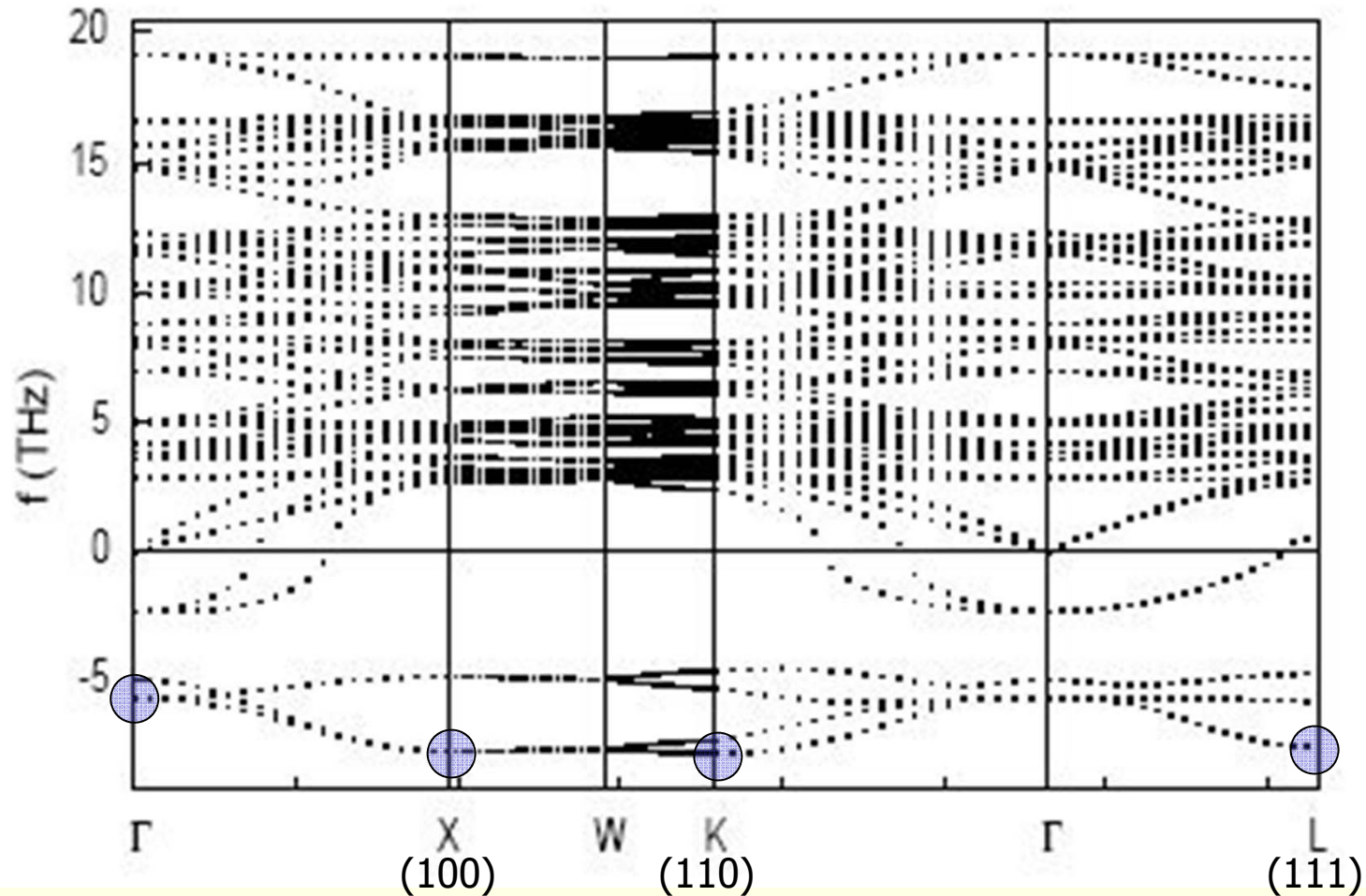
How could one obtain a non-magnetic insulator ?



- **Antiferromagnetic $s=1/2$ solution**
 - *(on geometrically frustrated lattice !?)*
- **Localization, strong e^-e^- correlation:**
 - *4d (not 3d !) electrons,*
 - *thus correlation should be small (Hubbard- $U \sim 2-3$ eV)*
 - *LDA+ U with $U=6$ eV gives insulator (FM ground state, no AFM)*
 - *bandwidth of t_{2g} bands: 2.5 eV (similar to U)*
- **structural distortion, which breaks the dominant octahedral crystal field**
- **→ Search for phonon-instabilities**
 - *88 atom supercell, 46 symmetry adapted selected distortions from PHONON; resulting forces → back into PHONON*



Phonon-bandstructure of $Y_2Nb_2O_7$

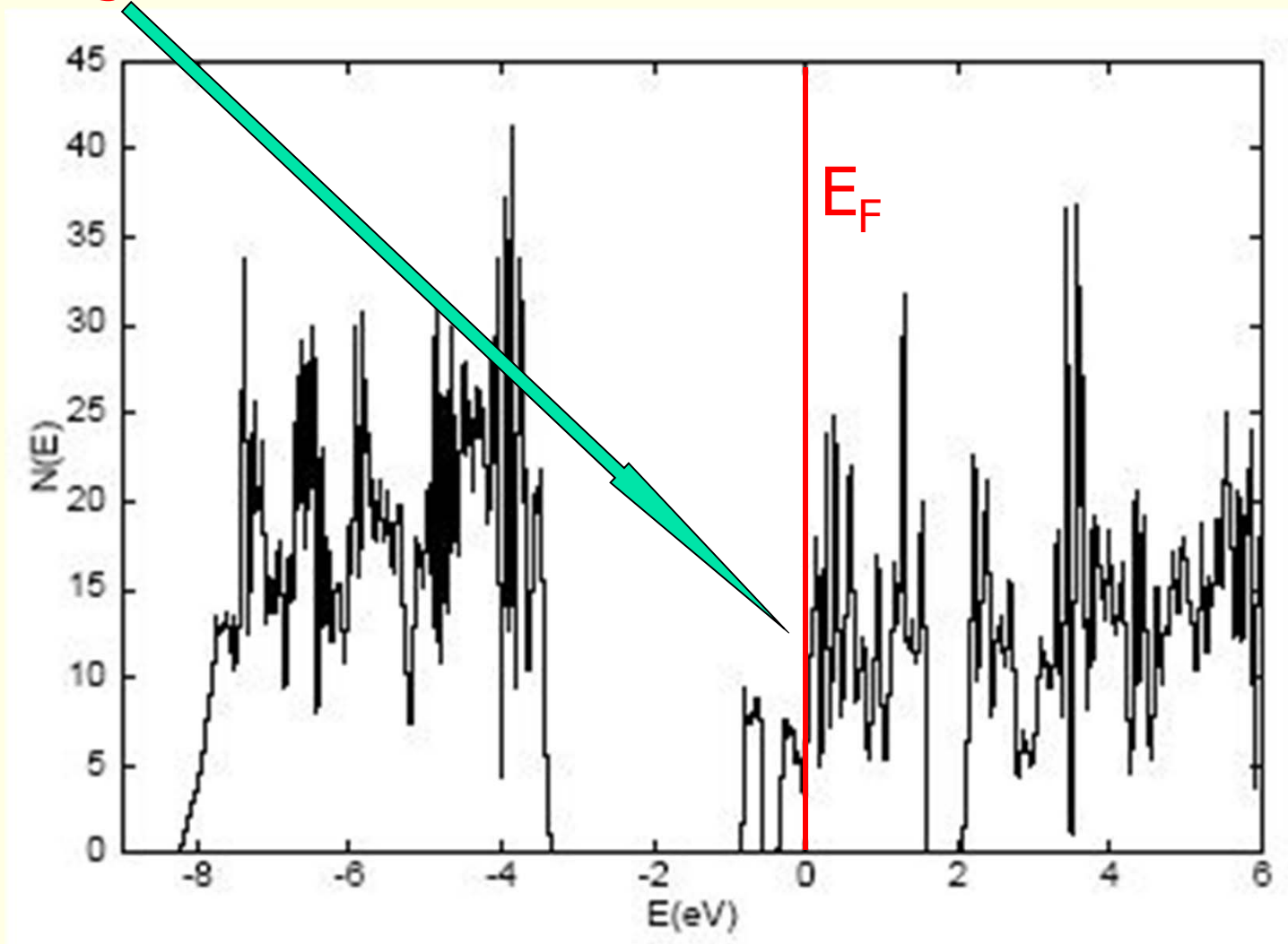


- strong Phonon-instabilities, lowest at X, K, L
- select a certain (unstable) phonon, freeze it into the structure with a certain amplitude and perform full structural optimization



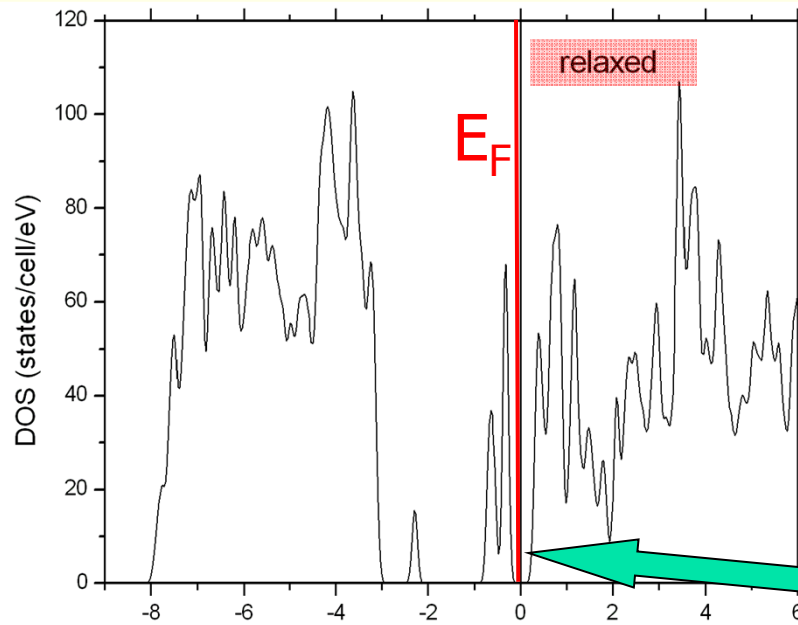
Γ , X and K-point phonons:

- energy lower than in ideal pyrochlore structure, but still not insulating



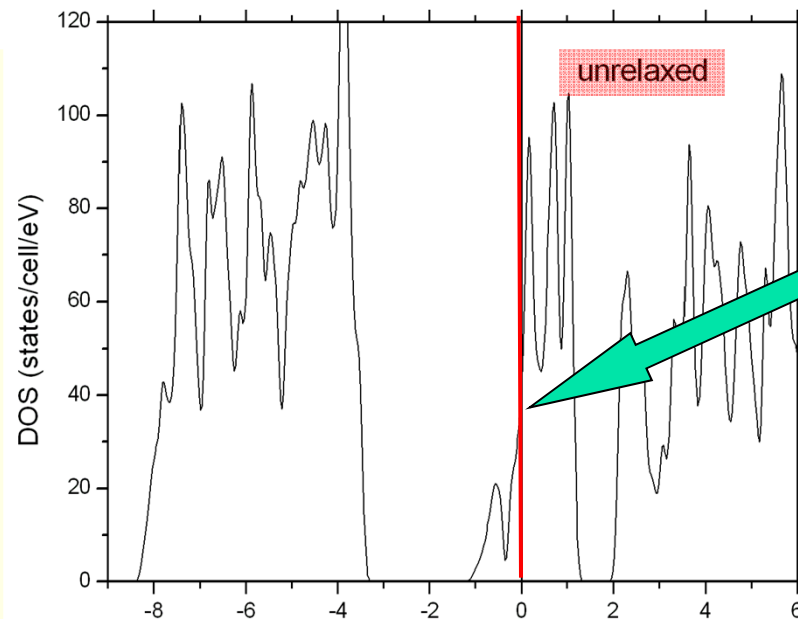


L-point (111) phonon:



- Relaxed structure is an **Insulator**
- energy gain of 0.5 eV/FU

gap



metal



Relaxed structure:



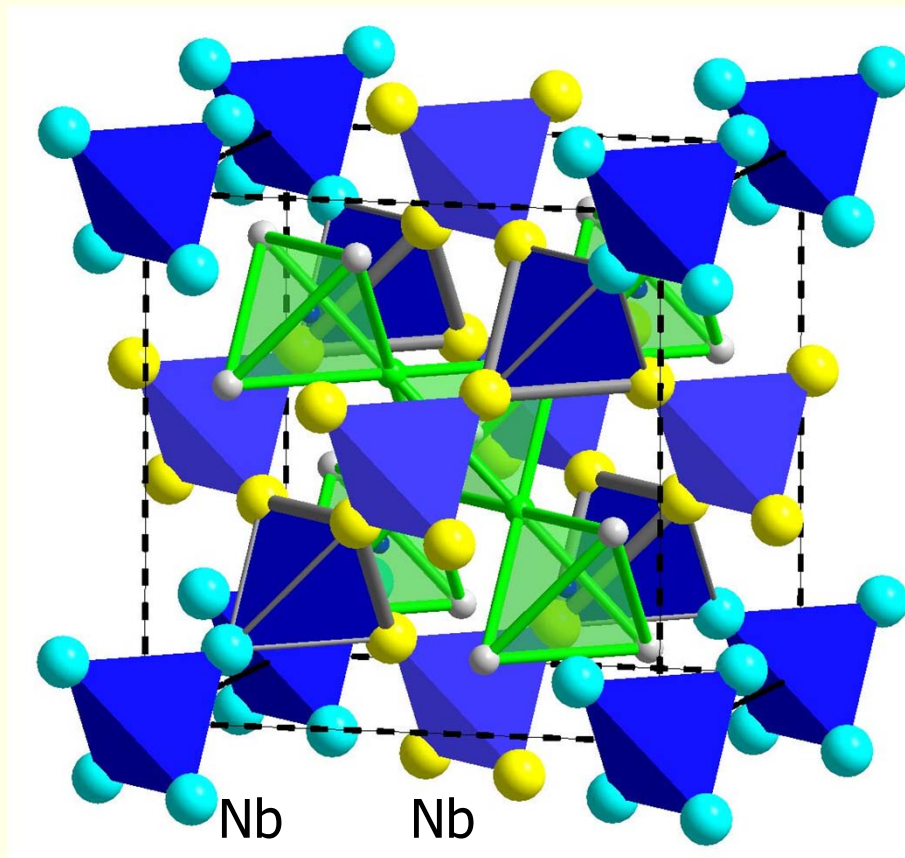
- Primitive supercell with 88 atoms
- all atoms inequivalent
 - due to numerical optimization of the positions in P1
- **Symmetrization using KPLOT** (R.Hundt, J.C.Schön, A.Hannemann, M.Jansen: *Determination of symmetries and idealized cell parameters for simulated structures, J.Appl.Cryst. 32, 413-416 (1999)*)
 - *Tests possible symmetries with increasing tolerance*
- Space group → P-43m, 88 atoms/cell,
 - *Inequivalent atoms:*
 - 2 Y
 - 2 Nb
 - 3 O1
 - 5 O2



Main change in structural relaxation

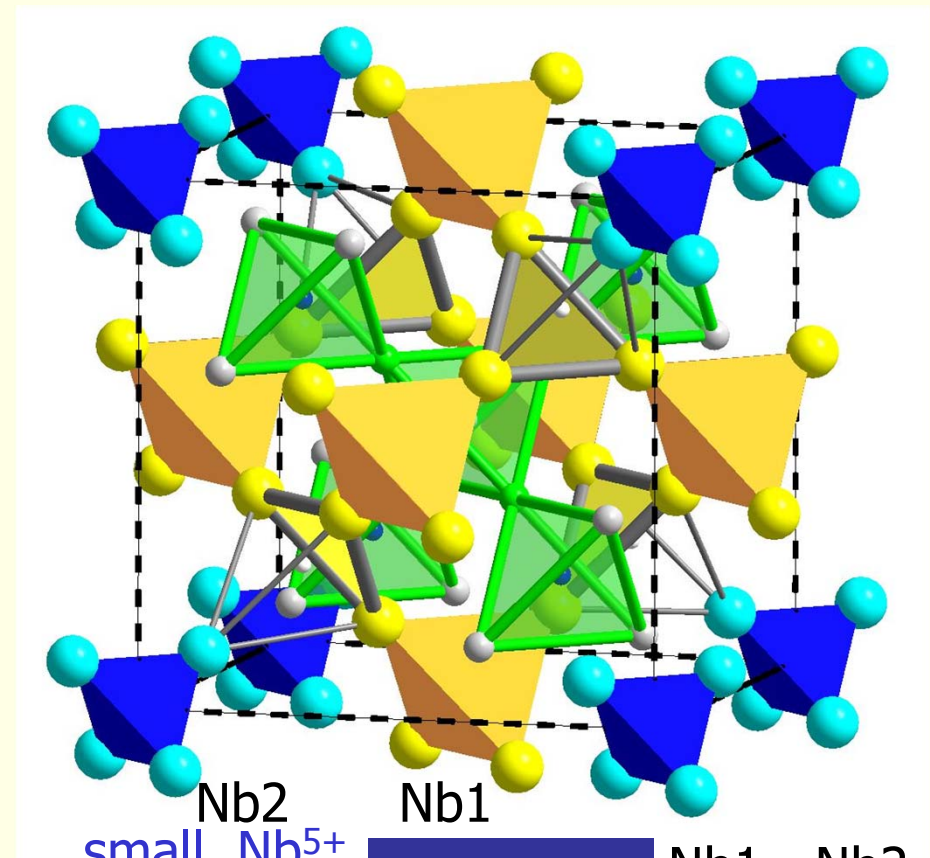


Original pyrochlore



3.65 Å equal, Nb⁴⁺

Relaxed structure

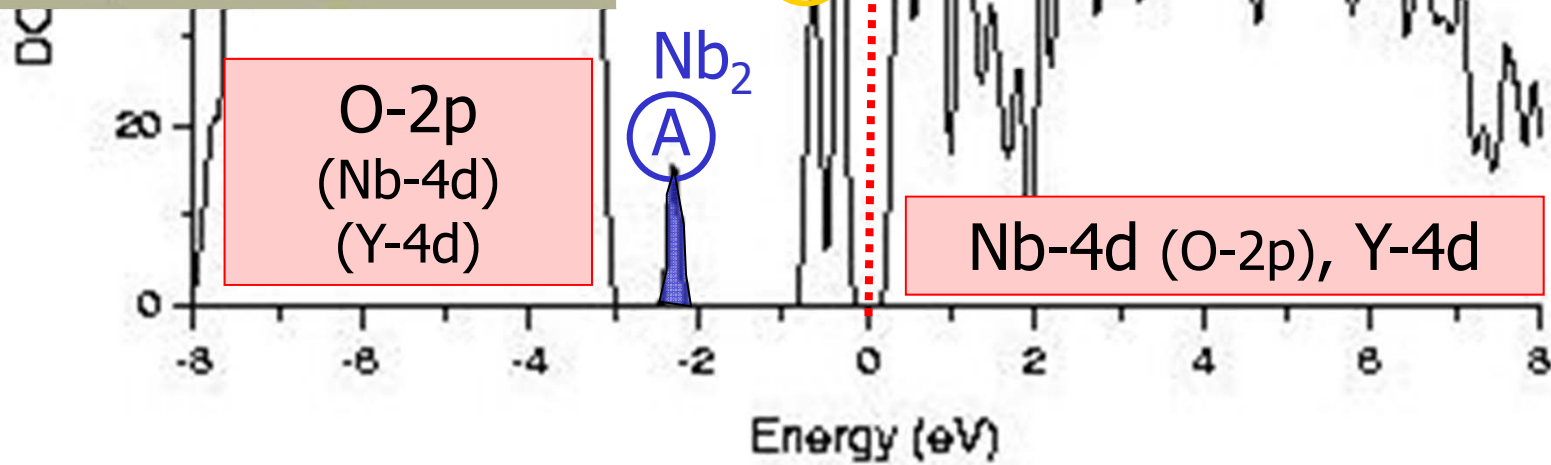
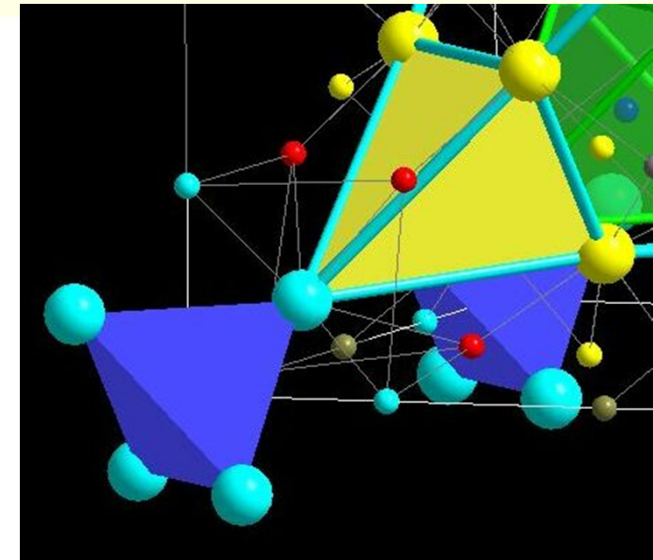
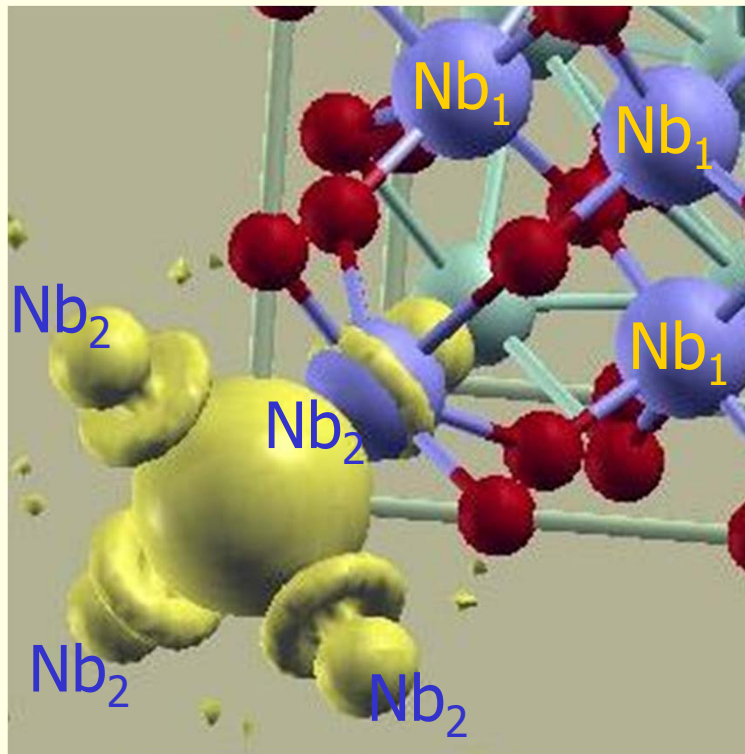


Nb2 small, Nb⁵⁺ 2.91 Å
Nb1 large Nb³⁺ 3.90 Å
Nb1 - Nb2 3.89 Å

Nb1-triangle: 3.40 Å



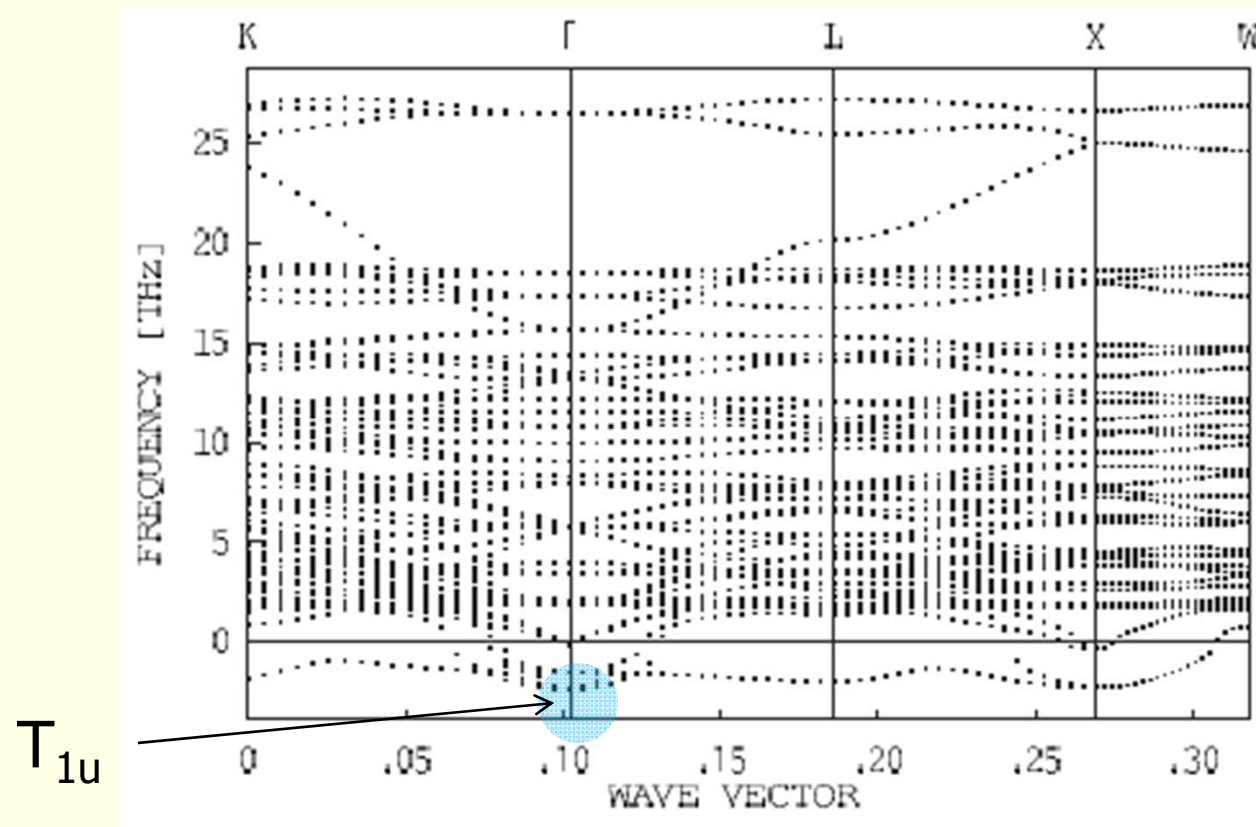
Peak A (Nb_2) 4-center bond ($d\text{-}z^2$)





$\text{Cd}_2\text{Nb}_2\text{O}_7$

- cubic pyrochlore structure, Nb^{5+} , insulator
- on cooling several PT starting below 205 - 45 K
- ferroelectric transition at 196 K



- Fischer et al. PRB 78, 014108 (2008)



frozen in T_{1u} mode

- structural optimization leads to Cc structure, but distortions from $Ima2$ are very small suggesting a sequence of PT
- $Fd\bar{3}m - Ima2 - Cc$

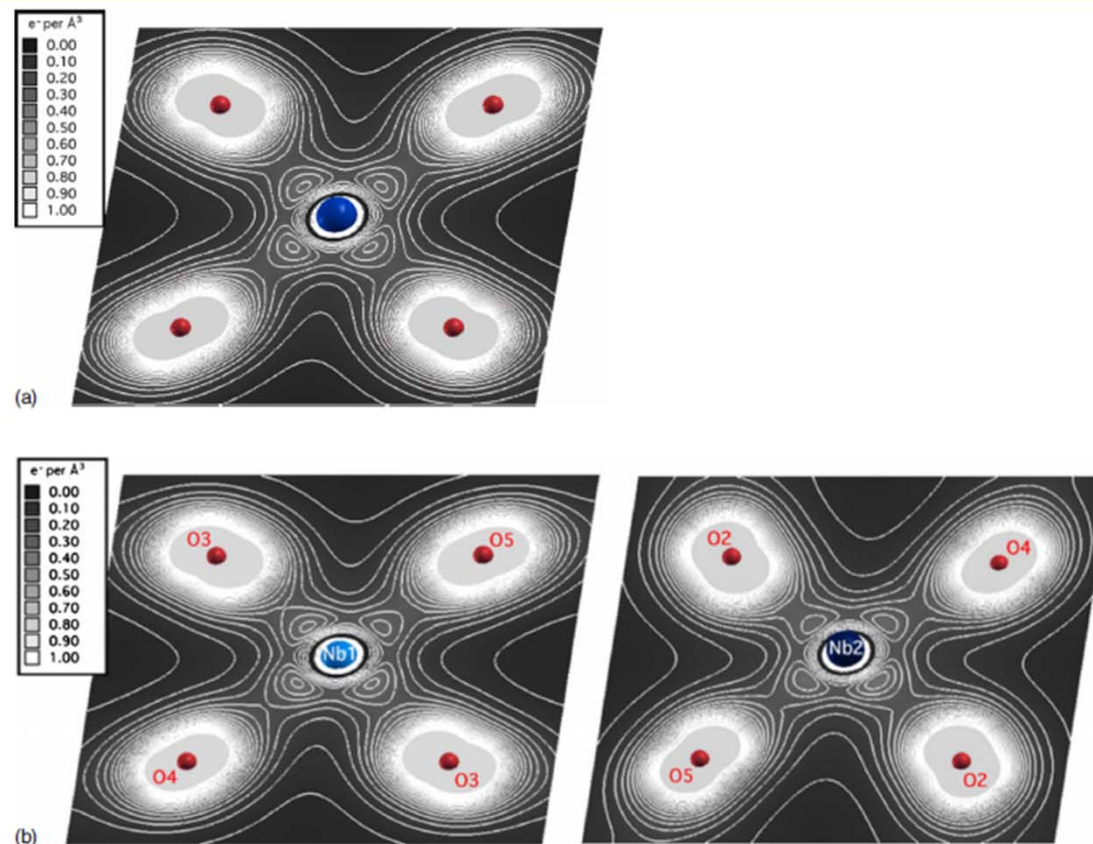


FIG. 6. (Color online) Electron-density maps for the energy region of Nb-O d - p bonding ($-5.55 \text{ eV} < E < -2.83 \text{ eV}$) in the $Fd\bar{3}m$ phase (a) and in the $Ima2$ phase (b). Isolines are in equal steps of $\approx 0.05e \text{ \AA}^{-3}$.



Conclusions



- The DFT approximation influences the results !
- WIEN2k is an accurate all-electron tool to understand solids
 - *electronic and geometric structure*
 - *interpretation of experiments (spectra)*
- Together with PHONON you can calculate phonons also in rather complicated structures
- Use “phonons” not only to match with experiment but to investigate interesting physics
 - *phase transitions, phase stability*
 - *search for unknown structures*

Thank you for
your attention !